

# Multi-Area Optimal Power Flow with Changeable Transmission Topology

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# Outline

- **I. Background**
- **II. Multi-area optimal power flow with changeable transmission topology**
- **III. Implement static switching security and N-k branch outage analysis on high performance computer**
- **V. Summary and future work**



# Introduction

- **Transmission switching: change and control transmission topology during operation**
- **Applications and Benefits**
  - Alleviate congestion and correct contingencies
  - Save production cost through changing the network topology during operations
- **Switching security**
  - Static switching security at the moment of switching operation
  - Transient state analysis
- **Computational issue**
  - Mixed integer programming formulation with big-M constraints, disjunctive programming formulation or nonlinear programming



# Past Work

## ■ Optimal transmission switching and unit commitment

O'Neill (2005), Dispatchable transmission in RTO markets, *IEEE Trans. Power System*.

Hedman (2010), Optimization of generation unit commitment and transmission switching with N-1 reliability, *IEEE Trans. Power System*.

Khodaei (2010), Transmission switching in security-constrained unit commitment, *IEEE Trans. Power System*.

## ■ Corrective switching

Shao (2008), Corrective switching algorithm for relieving overloads and voltage violations, *IEEE Trans. Power System*.

Hedman (2011), Smart Flexible Just-in-Time Transmission and Flowgate Bidding, *IEEE Trans. Power System*.

## ■ Static switching security

Liu (2012), Static switching security in multi-period transmission switching, *IEEE Trans. Power System*.

Ostrowski , anti-islanding in transmission switching, under revision.

## ■ Prescreening switchable lines and sequential LP

Fuller (2012), Fast heuristics for transmission-line switching, *IEEE Trans. Power System*.

Ruiz (2012), Tractable transmission control using sensitivity analysis, *IEEE Trans. Power System*.

Liu (2012), Heuristic prescreening switchable branches in optimal transmission switching, *IEEE Trans. Power System*, In press.



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# Multi-area Optimal Power Flow with Changeable Transmission Topology

## ■ Motivation

- Respect dispatching independence of each area in multi-area power systems. Limited information is exchanged among utilities or operating centers in different areas
- Optimal power flow with transmission switching is intractable even for moderately-sized power systems
- Perform computation in each region in parallel
- Potential use for multi-area network expansion or maintenance coordination



# Multi-area Optimal Power Flow with Changeable Transmission Topology

## Original Problem

$$\text{Min } f(x^A, y^A) + f(x^B, y^B)$$

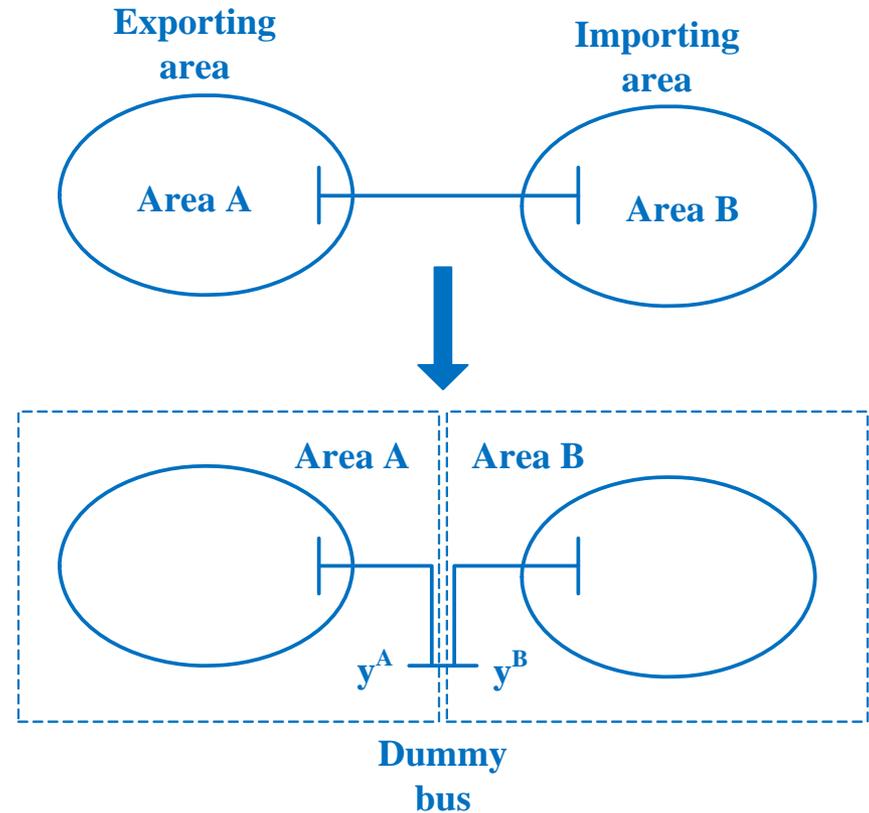
s.t.

Constraints for area A

Constraints for area B

Coupling constraints  $y^A = y^B$

$x^A$			
	$x^B$		
		.....	
			$x^N$
$y^A$	$y^B$	.....	$y^N$



# Lagrangian Relaxation

## ■ Area decomposition by Lagrangian relaxation

Lagrangian  
Function

$$\mathcal{L}(\mathbf{x}, \mathbf{y}, \boldsymbol{\lambda}) = f(\mathbf{x}^A, \mathbf{y}^A) + f(\mathbf{x}^B, \mathbf{y}^B) + \boldsymbol{\lambda}^T (\mathbf{y}^A - \mathbf{y}^B)$$

dual Function

$$\phi(\boldsymbol{\lambda}) = \underset{\mathbf{x}, \mathbf{y} \in S}{\text{Min}} f(\mathbf{x}^A, \mathbf{y}^A) + f(\mathbf{x}^B, \mathbf{y}^B) + \boldsymbol{\lambda}^T (\mathbf{y}^A - \mathbf{y}^B)$$

Dual problem

$$\underset{\boldsymbol{\lambda}}{\text{Max}} \underset{\mathbf{x}, \mathbf{y} \in S}{\text{Min}} f(\mathbf{x}^A, \mathbf{y}^A) + f(\mathbf{x}^B, \mathbf{y}^B) + \boldsymbol{\lambda}^T (\mathbf{y}^A - \mathbf{y}^B)$$

For given  $\boldsymbol{\lambda}$

$$\underset{\mathbf{x}^A, \mathbf{y}^A \in S^A}{\text{Min}} f(\mathbf{x}^A, \mathbf{y}^A) + \boldsymbol{\lambda}^T \mathbf{y}^A$$

Dual problem is  
decomposed

$$\underset{\mathbf{x}^B, \mathbf{y}^B \in S^B}{\text{Min}} f(\mathbf{x}^B, \mathbf{y}^B) - \boldsymbol{\lambda}^T \mathbf{y}^B$$

Updated Lagrangian  
multiplier

$$\boldsymbol{\lambda}^{(k+1)} = \boldsymbol{\lambda}^{(k)} + \eta^{(k)} \cdot (\mathbf{y}^A - \mathbf{y}^B)$$

Lower bound

$$\phi(\boldsymbol{\lambda}^{(k)}) \leq \phi(\boldsymbol{\lambda}^*) \leq f(\mathbf{x}^{A*}, \mathbf{y}^{A*}) + f(\mathbf{x}^{B*}, \mathbf{y}^{B*})$$



# Augmented Lagrangian Relaxation

- **Augmented Lagrangian function**

Introduce  
quadratic  
penalty term

$$\mathcal{A}(\mathbf{x}, \mathbf{y}, \boldsymbol{\omega}, \boldsymbol{\lambda}) = f(\mathbf{x}^A, \mathbf{y}^A) + f(\mathbf{x}^B, \mathbf{y}^B) + \boldsymbol{\lambda}^T (\mathbf{y}^A - \mathbf{y}^B) + \boldsymbol{\omega} \|\mathbf{y}^A - \mathbf{y}^B\|^2$$

- **The augmented Lagrangian function cannot be decomposed as it contains an inseparable cross penalty term**
- **Augmented Lagrangian relaxation + Auxiliary problem principle**
- **Augmented Lagrangian relaxation + Block coordination decent**



# Augmented Lagrangian Relaxation

- **Augmented Lagrangian relaxation + Auxiliary Problem Principle**

- Use the results in the last iteration
- Update multipliers and penalty factors iteratively

$$\min_{\mathbf{x}^A, \mathbf{y}^A} f(\mathbf{x}^A, \mathbf{y}^A) + \boldsymbol{\lambda}_k^T \mathbf{y}^A + \alpha(\mathbf{y}_k^A - \mathbf{y}_k^B)^T \mathbf{y}^A + \beta \|\mathbf{y}^A - \mathbf{y}_k^A\|^2$$

*s.t.* constraints in area A

$$\min_{\mathbf{x}^B, \mathbf{y}^B} f(\mathbf{x}^B, \mathbf{y}^B) - \boldsymbol{\lambda}_k^T \mathbf{y}^B + \alpha(\mathbf{y}_k^B - \mathbf{y}_k^A)^T \mathbf{y}^B + \beta \|\mathbf{y}^B - \mathbf{y}_k^B\|^2$$

*s.t.* constraints in area B

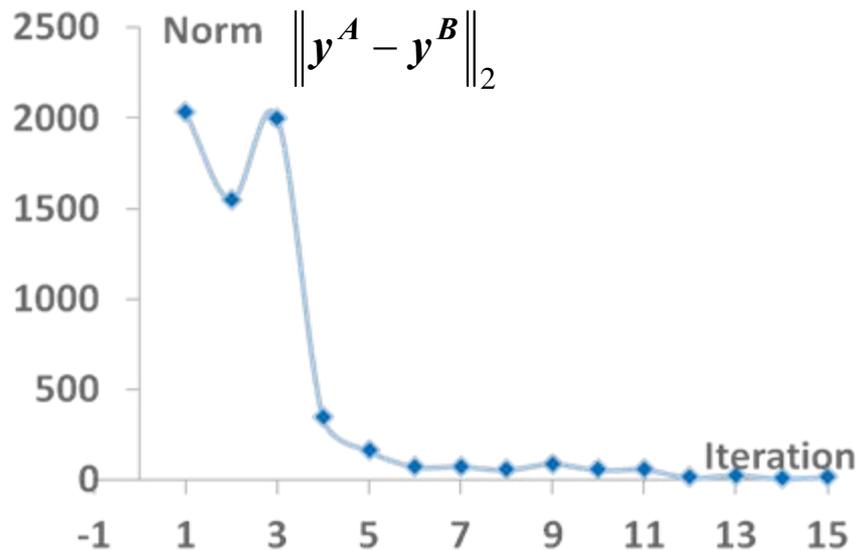
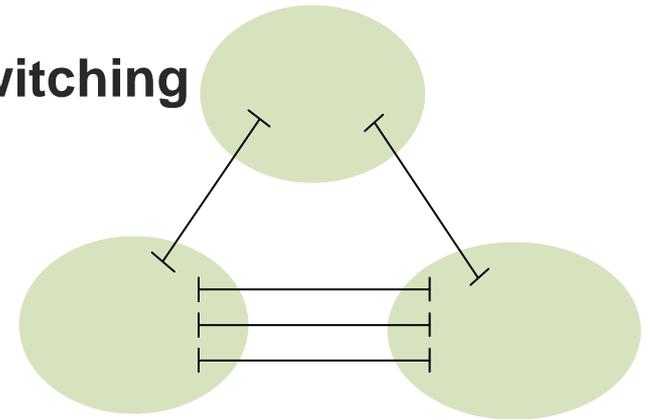
$$\boldsymbol{\lambda}_{k+1} = \boldsymbol{\lambda}_k + \gamma(\mathbf{y}_{k+1}^A - \mathbf{y}_{k+1}^B)$$

- **The program stops if the norm is less than a given value**

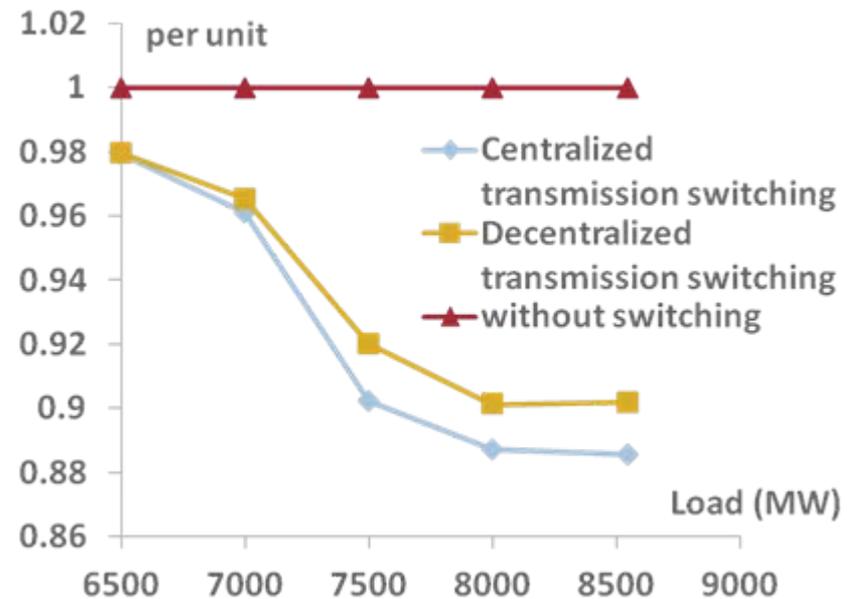


# Preliminary Testing Results

- Modified RTS system for transmission switching
- 3 areas, 5 tie-lines
- 117 branches, 111 Units
- No anti-islanding constraints
- Load 6500MW - 8547MW



Norm of violation of constraints in dual solution



Production cost comparison



# Preliminary Testing Results

- Larger systems
- Solve the problem with centralized method to optimality

Case		Decentralized method (ALR)					Centralized method
Areas	Buses	Branches	Load (MW)	Number of tie-lines	Wall-clock time (s)	Operating cost reduction	Operating cost reduction
6	146	236	16600	12	43	7.1%	7.3%
9	219	354	24900	18	79	6.2%	6.3%
12	292	472	33200	24	202	7.4%	7.6%



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# SCOPF with post-contingency correction

$$\mathbf{x}^* \left\{ \begin{array}{l} \mathbf{x}^0 \left\{ \begin{array}{l} \text{Min} \quad f(\mathbf{x}) \\ \text{S.t.} \quad \mathbf{A} \cdot \mathbf{x} \leq \mathbf{b} \end{array} \right. \\ \begin{array}{l} g(\mathbf{x}, \mathbf{y}) \leq 0 \\ g(\mathbf{x}^c, \mathbf{y}^c) \leq 0 \\ |\mathbf{x} - \mathbf{x}^c| \leq \Delta \end{array} \end{array} \right.$$

Objective

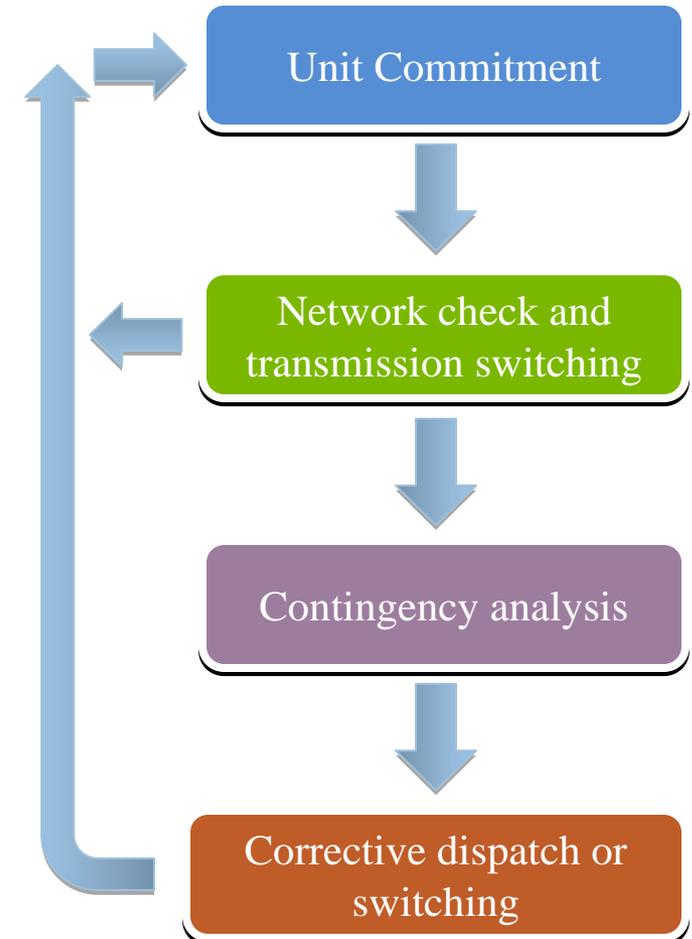
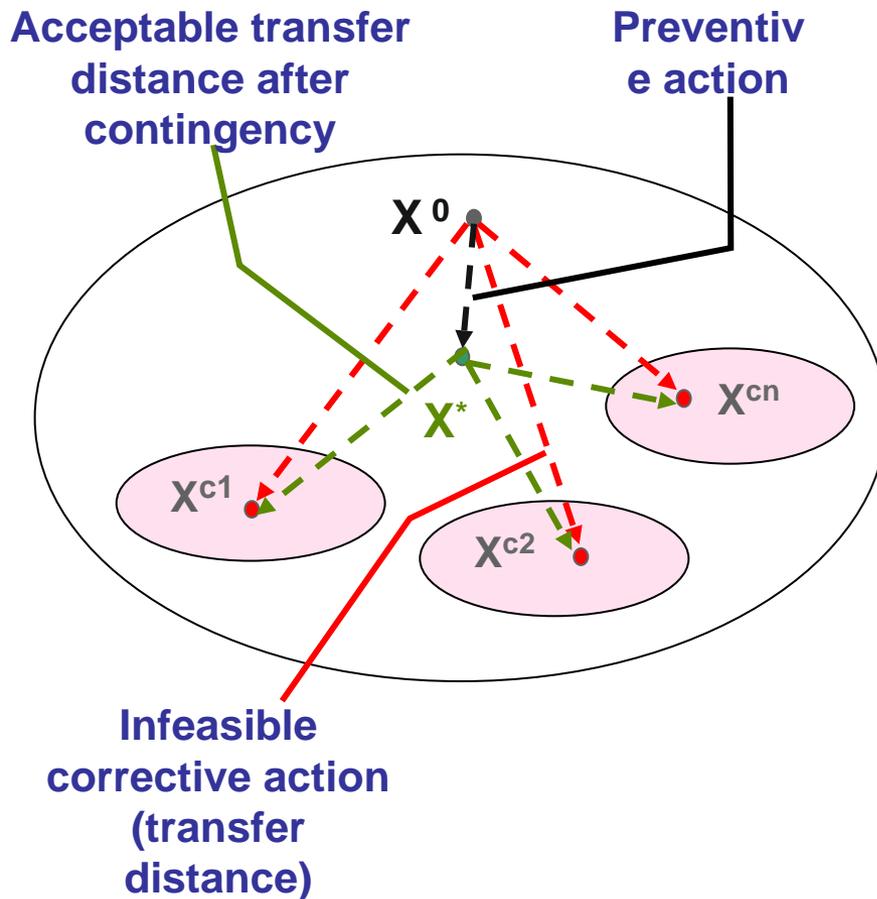
Unit commitment and economic dispatch constraints

Network constraints in normal state

Network constraints after each contingency

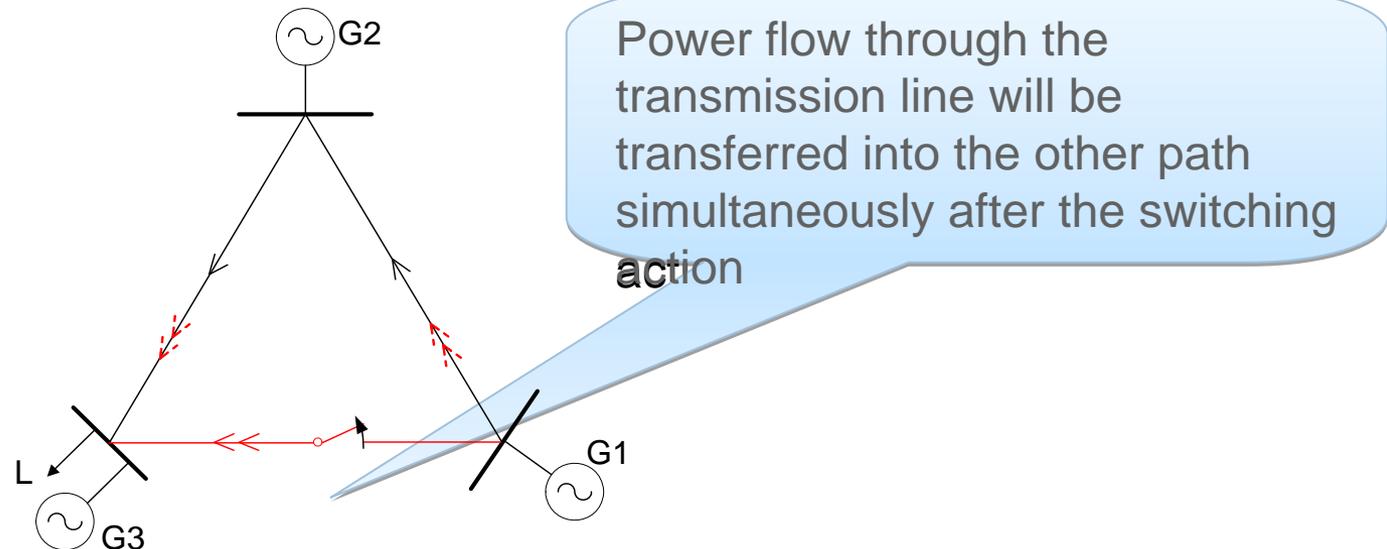
Transfer distance constraints

# Corrective and preventive actions in power system operations



# Static Switching Security of transmission switching

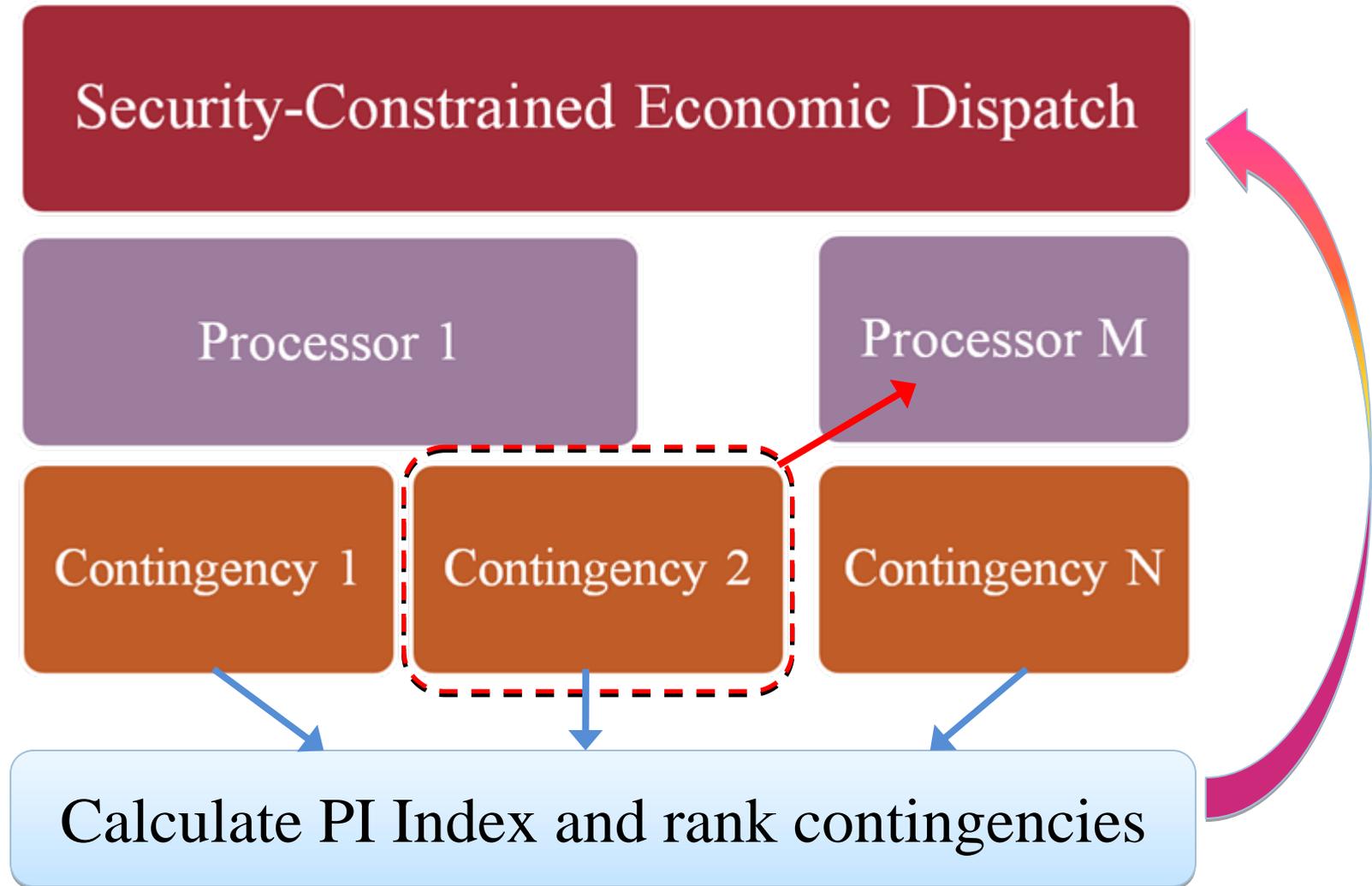
- Electromagnetic transients process is very fast. The instant redistribution of power flow and voltage during switching operations may violate normal or emergency rates of transmission lines



- N-k line open or close operations



# Parallelism for Contingency analysis

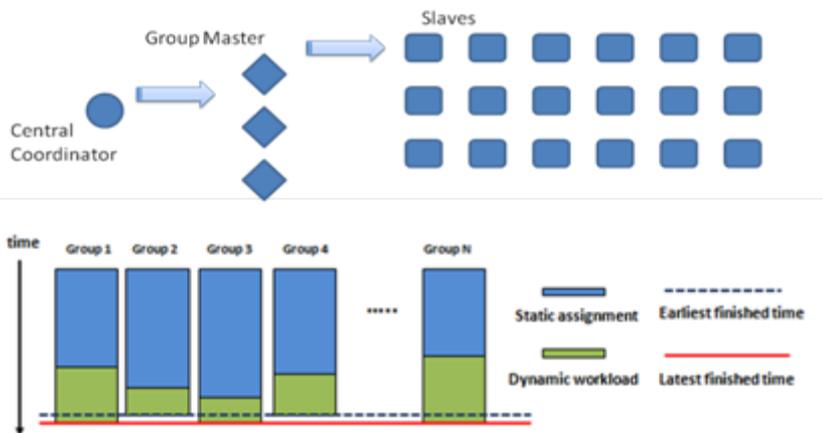


# N-k Line Switching and Outage Analysis using HPC

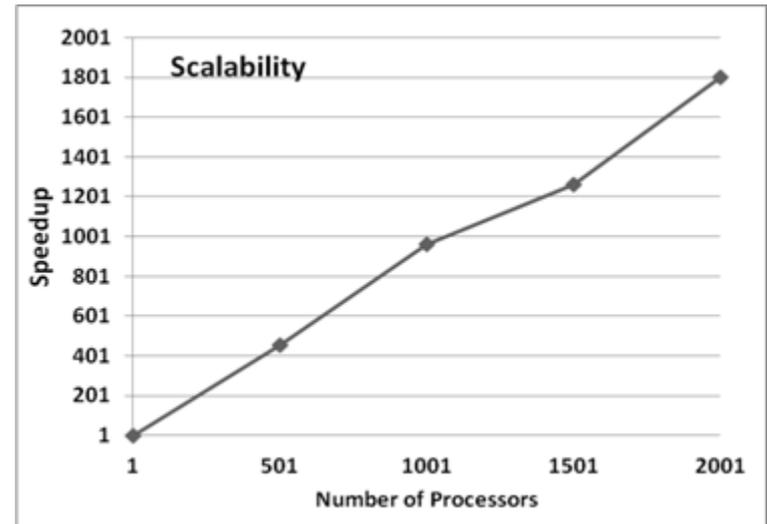
Communication becomes a bottleneck for improving scalability

- 1168 bus system
- All N-1 and N-2 cases
- AC power flow

## Three-Layered Dynamic Scheduling



Working load balance



## Scalability of N-k line outage analysis

- We have already tested a 14000-bus system. And we will report the results soon



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# Summary and Future Work

- **A multi-area optimal power flow with changeable topology is used for coordinating the decision making in each area**
- **Implement larger case study**
- **Decentralized scheduling of planning and maintenance in multi-area optimization framework**
- **Continue implementing contingency analysis on high performance computer**
- **Link contingency analysis with the parallel implementation of optimal power flow**



**Thank you! Questions?**

