

N-1-1 Contingency-Constrained Grid Operations

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Increasing Real-Time and Day-Ahead Market Efficiency through
Improved Software

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Reliability of Power Systems

- In recent years, the number of large blackouts have been on the rise. For examples:
 - June 2012 India (over 620 million people affected)
 - Sept. 2011 Southwest, USA (initiating event by loss of a 500kV line)
- Growing complexity of power systems: distributed generations and significant generation uncertainty
- Systems operating closer to feasibility limits are more vulnerable to failures, due to natural causes and/or intelligent adversaries.
- **Survivability**: system's ability to survive imminent disturbances (contingencies) without interruption of customer service

North American Electric Reliability Corporation (NERC):

- develop and enforce standards to ensure the reliability of the power systems in North America

Transmission planners and planning coordinators:

- prepare necessary performance assessments for their portion of the system under different contingency conditions
- ensure that system complies with approved NERC TPL standards

Transmission Planning Standard (TPL-001-1): system performance requirements under both normal and various contingency conditions

- No contingencies (Category A)
- Events resulting in the loss of a single system element (Category B)
- Event(s) resulting in the loss of two or more elements (Category C)
- Extreme event resulting in two or more elements removed or cascading out of service (Category D)

TPL-001-1 standards

Category	System Stable	Loss of Demand	Cascading Outages
$N-0$	Yes	No	No
$N-1$	Yes	No	No
$N-k$	Yes	Planned/Controlled	No
$N-1-1$	Yes	Planned/Controlled	No

- Category B events: loss of a single system component
 - $N-1$ contingency
- Category C events: loss of two or more components
 - (near-)simultaneous losses: $N-k$ ($k \geq 2$) contingency
 - Consecutive losses: $N-1-1$ contingency

Contingency Analysis

- Contingency analysis: a key function in the Energy Management System
- $N-1$ contingency analysis:
 - system to operate under normal conditions (per TPL-001-1)
 - not sufficient to model/evaluate vulnerabilities of power grids
 - $N-1$ reliability analysis: UC with transmission switching (Hedman et al. 2010)

Contingency Analysis

- Contingency analysis: a key function in the Energy Management System
- $N-k$ contingency analysis:
 - a substantial computational burden for analysis, $\sum_{i=1}^k \binom{N}{i}$
 - vulnerability analysis (Pinar et al. 2010, Bienstock et al. 2010)
 - power flow (Salmeron et al. 2004, Arroya 2010, Fan et al. 2010)
 - survivable power system design (Chen et al. 2012)
 - contingency-constrained unit commitment (Chen et al. 2013)
 - robust unit commitment (Street et al. 2011, Wang et al. 2012)

Contingency Analysis

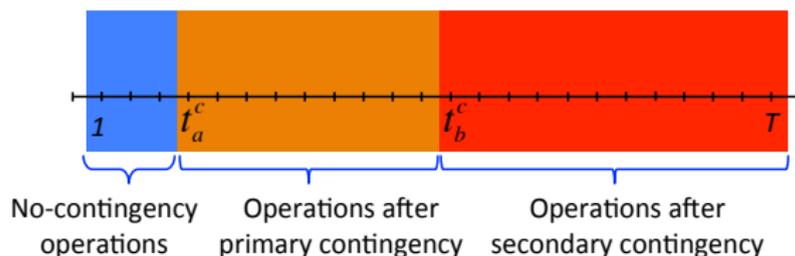
- Contingency analysis: a key function in the Energy Management System
- *N-1-1* contingency analysis:
 - a category B event followed by a category C event per TPL-001-1
 - simulation analysis: PowerWorld, Mathwork, Siemens Energy (2011), Chatterjee et al. (2010) for midwest ISO
 - optimal power flow (Fan et al. 2012)

$N-1-1$ Contingency-Constrained Unit Commitment

- Baseline UC: find least cost on/off schedule of generating units and economic dispatch (DCOPF) to meet electrical loads
- $N-1-1$ CCUC: find expected, least-cost on/off schedule of generating units, economic dispatch (DCOPF) such that a feasible recourse DC PF exist for any $N-1-1$ contingency state
- Modeled as a three-stage stochastic mixed-integer program (SMIP)

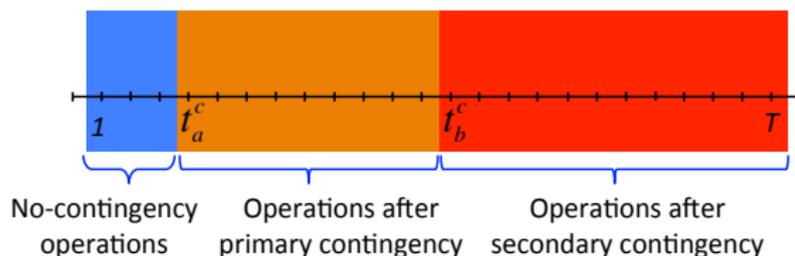
Time periods

- given a $N-1-1$ contingency state c
- planning horizon T
- t_a^c, t_b^c , times of the primary and secondary contingencies, respectively



Time periods

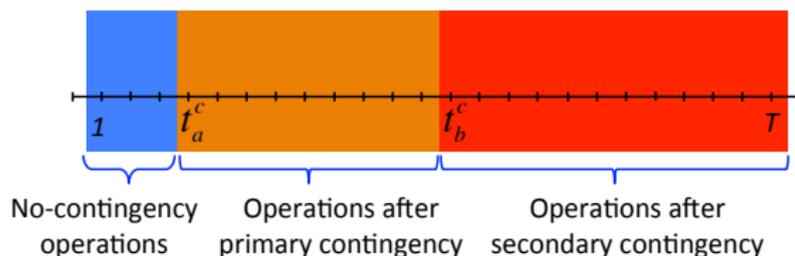
- given a $N-1-1$ contingency state c
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- non-anticipativity during no-contingency operations

Time periods

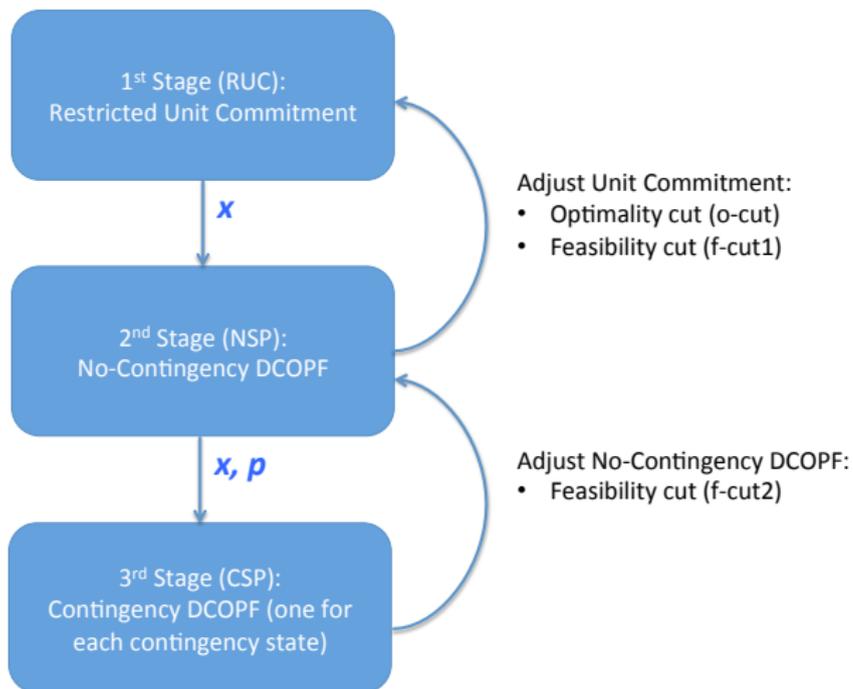
- given a $N-1-1$ contingency state c
- planning horizon T
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- non-anticipativity during no-contingency operations
- line overload and loss-of-load permitted during secondary contingency state

Three-Stage $N-1-1$ UC Model

Three-stage model/Nested Benders decomposition



Indices and parameters:

- Planning horizon, $\mathcal{T} = \{1, \dots, T\}$
- Power system ($i \in N, g \in G, e \in E$):
 - T_g^{u0}, T_g^{d0} , initial online and offline
 - T_g^u, T_g^d , minimum online and offline

Decision variables:

- $x_g^t \in \{0, 1\}$, generator on/off

Three-Stage Formulation: 1st stage (RUC)

- objective: minimize startup, shutdown costs, and no-contingency state generation cost
- constraints:
 - minimum online/offline requirements (initial periods)
 - minimum online/offline requirements
 - startup/shutdown costs
- variables: $x_g^t \in \{0, 1\} \quad \forall, g \in G, t \in \mathcal{T}$
- UC formulation based on Carrion and Arroyo (2006) and Wu and Shahidehpour (2010)

Indices and parameters:

- Power system ($i \in N, g \in G, e \in E$):
 - i_e, j_e , tail and head bus of line e
 - D_i^t , demand
 - $\underline{P}_g, \bar{P}_g$, generation bounds
 - $R_g^u, R_g^d, \bar{R}_g^u, \bar{R}_g^d$, ramp rates
 - B_e, F_e , susceptance and capacity

Decision variables:

- p_g^t, f_e^t, θ_i^t , no-contingency state generation level, flow, and voltage phase angle

Three-Stage Formulation: 2nd stage (NSP)

$$\min \sum_{t \in \mathcal{T}} \sum_{g \in G} C_g^p(p_g^t)$$

$$\text{s.t.} \quad \sum_{g \in G_i} p_g^t + \sum_{e \in E_i} f_e^t - \sum_{e \in E_i} f_e^t = D_i^t, \quad \forall i, t$$

$$B_e(\theta_{i_e}^t - \theta_{j_e}^t) - f_e^t = 0, \quad \forall e, t$$

$$-F_e \leq f_e^t \leq F_e, \quad \forall e, t$$

$$\underline{P}_g \tilde{x}_g^t \leq p_g^t \leq \bar{P}_g \tilde{x}_g^t, \quad \forall g, t$$

$$p_g^t - p_g^{s,t-1} \leq R_g^u \tilde{x}_g^{t-1} + \bar{R}_g^u (\tilde{x}_g^t - \tilde{x}_g^{t-1}) \\ + \bar{P}_g (1 - \tilde{x}_g^t), \quad \forall g, t$$

$$p_g^{s,t-1} - p_g^t \leq R_g^d \tilde{x}_g^t + \bar{R}_g^d (\tilde{x}_g^{t-1} - \tilde{x}_g^t) \\ + \bar{P}_g (1 - \tilde{x}_g^{t-1}), \quad \forall g, t$$

- minimize generation cost
- power balance at each bus
- power flow w.r.t. phase angles
- line capacity bounds
- generation capacity bounds
- generation ramp-up
- generation ramp-down

Indices and parameters:

- Power system ($i \in N, g \in G, e \in E$):
 - \mathcal{C} , set of all $N-1-1$ contingencies (indexed by c)
 - $\tilde{d}_e^{ct}, \tilde{d}_g^{ct}$, contingency element indicators
 - t_a^c, t_b^c , times of the primary and secondary contingency for c , respectively
 - \tilde{v}_2^{ct} , in secondary contingency indicator, \tilde{v}_2^{ct} equal 1 for all $t > t_b$ and 0 otherwise
 - o_e , allowable line overload factor during secondary contingency state

Decision variables:

- $p_g^{ct}, f_e^{ct}, \theta_i^{ct}, q_i^{ct}$, contingency state c generation level, flow, voltage phase angle, loss-of-load

$N-1-1$ contingency set (\mathcal{C})

- refers to the loss of a system element followed by a loss of another system element in a subsequent time period
- in a given time period at most one element in $G \cup E$ can fail
- there are $\binom{T}{2} = \frac{T(T-1)}{2}$ possible pairs of periods for primary and secondary losses
- $|G| + |E|$ possible losses for primary contingency
- $|G| + |E| - 1$ possible losses for secondary contingency
- $|\mathcal{C}| = \frac{T(T-1)}{2} (|G| + |E|)(|G| + |E| - 1)$
- number of $N-2$ contingencies = $\frac{(|G|+|E|)(|G|+|E|-1)}{2}$

Three-Stage Formulation: 3rd stage (CSP)

Recourse operations in contingency state c , for all $c \in \mathcal{C}$ and $t = t_a^c, \dots, T$,

$$\sum_{g \in G_i} p_g^{ct} + \sum_{e \in E_i} f_e^{ct} - \sum_{e \in E_i} f_e^{ct} + q_i^{ct} = D_i^t, \forall i, t$$

- power balance at each bus

$$B_e(\theta_{i_e}^{ct} - \theta_{j_e}^{ct})(1 - \sum_{t'=t_a^c}^t \tilde{d}_e^{ct'}) - f_e^{ct} = 0, \forall e, t$$

- power flow w.r.t. phase angles

$$-f_e^{ct} \leq F_e(1 - \sum_{t'=t_a^c}^t \tilde{d}_e^{ct'})(1 + o_e \tilde{v}_2^{ct}), \forall e, t$$

- line capacity bounds

$$f_e^{ct} \leq F_e(1 - \sum_{t'=t_a^c}^t \tilde{d}_e^{ct'})(1 + o_e \tilde{v}_2^{ct}), \forall e, t$$

$$-p_g^{ct} \leq \underline{P}_g \tilde{x}_g^t (1 - \sum_{t'=t_a^c}^t \tilde{d}_g^{ct'}), \forall g, t$$

- generation capacity bounds

$$p_g^{ct} \leq \bar{P}_g \tilde{x}_g^t (1 - \sum_{t'=t_a^c}^t \tilde{d}_g^{ct'}), \forall g, t$$

Three-Stage Formulation: 3rd stage (CSP)

$$p_g^{ct} - p_g^{c,t-1} \leq R_g^u \tilde{x}_g^{t-1} + \bar{R}_g^u (\tilde{x}_g^t - \tilde{x}_g^{t-1}) + \bar{P}_g (1 - \tilde{x}_g^t), \forall g, t$$

- generation ramp-up

$$p_g^{c,t-1} (1 - \sum_{t'=t_0^c}^t \tilde{d}_g^{ct'}) - p_g^{ct} \leq R_g^d \tilde{x}_g^t + \bar{R}_g^d (\tilde{x}_g^{t-1} - \tilde{x}_g^t) + \bar{P}_g (1 - \tilde{x}_g^{t-1}), \forall g, t$$

- generation ramp-down

$$0 \leq q_i^{ct} \leq D_i^t, \forall i, t$$
$$\sum_{i \in V} q_i^{ct} \leq (\varepsilon \sum_{i \in V} D_i^t) \tilde{v}_2^{ct}, \forall i, t$$

- load shedding threshold

$$p_g^{c,t_0^c-1} = \tilde{p}_g^{t_0^c-1}, \forall g \in G \mid \tilde{d}_g^{t_0^c} = 0$$

- non-anticipativity

Dualize constraints above to form a maximization problem. If infeasible the dual is unbounded.

Optimality and Feasibility Cuts

If $\text{NSP}(\tilde{x})$ is feasible, an optimality cut can be generated.

$$[\text{o-cut}] : \delta^T x + \gamma_1 \leq Q$$

If $\text{NSP}(\tilde{x})$ is infeasible, the dual problem is unbounded and a feasibility cut can be generated.

$$[\text{f-cut1}] : \delta^T x + \gamma_1 \leq 0$$

If $\text{CSP}(\tilde{x}, \tilde{p}, c)$ is infeasible, the dual problem is unbounded and a feasibility cut can be generated.

$$[\text{f-cut2}] : \alpha^T p + \gamma_2 \leq 0$$

Power System Inhibition Problem - PSIP($\tilde{x}, \tilde{p}, t_a, t_b$)

For $t = t_a, \dots, T$,

$$\max_{d^{t_a}, d^{t_b}} \min_{f, p, q, r, s, \theta} \sum_t \sum_g r_g^t + \sum_t s^t$$

$$\text{s.t. } \sum_e d_e^{t_a} + \sum_g d_g^{t_a} = 1$$

$$\sum_e d_e^{t_b} + \sum_g d_g^{t_b} = 1$$

$$\sum_t d_e^t = 1, \forall e$$

$$\sum_t d_g^t = 1, \forall g$$

$$\sum_{g \in G_i} (p_g^t - r_g^t) + \sum_{e \in E_i} f_e^t - \sum_{e \in E_i} f_e^t + q_i^t = D_i^t, \forall i, t$$

$$B_e(\theta_{i_e}^t - \theta_{j_e}^t)(1 - \sum_{t'=t_a}^t d_e^{t'}) - f_e^t = 0, \forall e, t$$

$$-f_e^t \leq F_e(1 - \sum_{t'=t_a}^t d_e^{t'})(1 + o_e \tilde{v}_2^t), \forall e, t$$

$$f_e^t \leq F_e(1 - \sum_{t'=t_a}^t d_e^{t'})(1 + o_e \tilde{v}_2^t), \forall e, t$$

- minimize load and generation shedding above allowable threshold
- contingency constraints
- power balance at each bus
- power flow w.r.t. phase angles
- line capacity bounds

Power System Inhibition Problem (PSIP)

$$-p_g^t \leq \underline{P}_g \tilde{x}_g^t (1 - \sum_{t'=t_a}^t d_g^{t'}), \quad \forall g, t$$

$$p_g^t \leq \bar{P}_g \tilde{x}_g^t (1 - \sum_{t'=t_a}^t d_g^{t'}), \quad \forall g, t$$

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$$p_g^{t-1} - p_g^t \leq R_g^d \tilde{x}_g^t + \bar{R}_g^d (\tilde{x}_g^{t-1} - \tilde{x}_g^t) \\ + \bar{P}_g (1 - \tilde{x}_g^{t-1}), \quad \forall g, t$$

$$0 \leq q_i^t \leq D_i^t, \quad \forall i, t$$

$$\sum_{i \in V} q_i^t - (\varepsilon \sum_{i \in V} D_i^t) \tilde{v}_2^t \leq s^t, \quad \forall i, t$$

$$r_g^t \leq p_g^t, \quad \forall g, t$$

$$p_g^{t_a-1} = \tilde{p}_g^{t_a-1} (1 - d_g^{t_a}), \quad \forall g$$

$$d_e^t \in \{0, 1\}, d_g^t \in \{0, 1\}, \quad \forall t \in \{t_a, t_b\}$$

$$d_e^t = 0, d_g^t = 0, \quad \forall t \notin \{t_a, t_b\}$$

$$p_g^t \geq 0, r_g^t \geq 0, s^t \geq 0, \quad \forall g, t$$

- generation capacity bounds
- generation ramp-up
- generation ramp-down
- load and generation shedding
- non-anticipativity
- integrality restrictions
- non-negativity restrictions

- PSIP is a bilevel program and cannot be solved directly.
- PSIP can be reformulated as a MILP
 - bilinear terms in the objective
 - product of d^{t_a} , d^{t_b} and continuous lower level variables
 - mixed-integer linear reformulation referred to as PSIP-M

Cutting Plane Algorithm 2 (CPA2)

- 0: Initialize LB, UB
- 1: Solve RUC
- 2: If infeasible, EXIT
- 3: Else, update LB and solutions \tilde{x} , \tilde{Q}
- 4: Solve a NSP(\tilde{x}),
- 5: If infeasible, add [f-cut1] to RUC and go to (1)
- 6: Else, let \tilde{p} be the optimal generation schedule and z be the ofv
- 7: For each (t_a, t_b) pairs, solve PSIP-M($\tilde{x}, \tilde{p}, t_a, t_b$) and let w be the ofv
- 8: If $w > 0$, add [f-cut2] to NSP(\tilde{x}) and go to (4)
- 9: If $z > Q$, add [o-cut] to RUC
- 10: Update UB
- 11: If $(UB - LB < \epsilon)$, EXIT
- 12: Else, go to (1)

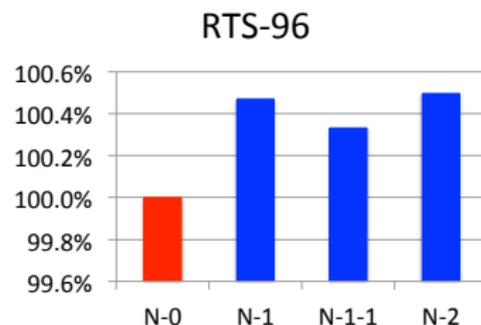
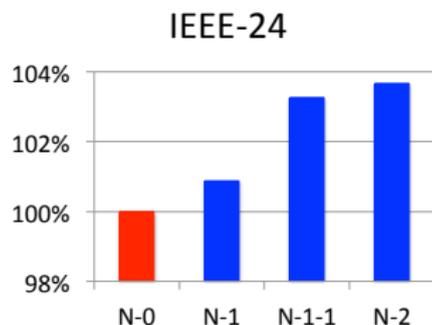
- At each iteration of CPA2:
 - Instead of solving $|\mathcal{C}|$ linear programs (CSP)
For $c \in \mathcal{C}$, solve $\text{CSP}(\tilde{x}, \tilde{p}, c)$
 - We now solve $\frac{1}{2}(T)(T - 1)$ mixed-integer linear programs (PSIP-M)
For each (t_a, t_b) pairs, solve $\text{PSIP-M}(\tilde{x}, \tilde{p}, t_a, t_b)$
- Number of contingencies identified is extremely small

Preliminary Study Setup

- Test Systems: modified IEEE-24 and RTS-96
- Time periods: $T = 6$
- Implementation C++, CPLEX 12.1 and Concert 2.9
- ϵ values of 0.08, and 0.05 for IEEE-24 and RTS-96, respectively
- Line overload factor $\sigma_e = 0.25$

Preliminary Observations (1 of 3)

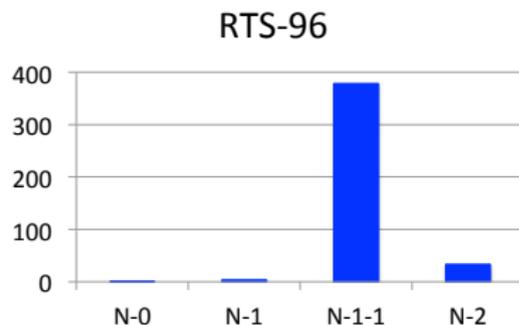
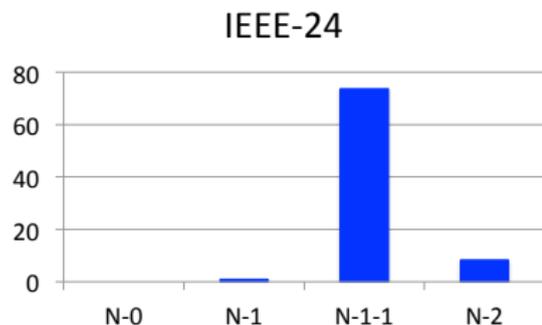
Cost comparison using N-0 as baseline



- Modest increases in costs
- Small number of contingencies identified (3 to 7)
- Contingencies mostly correspond to failures in consecutive periods

Preliminary Observations (2 of 3)

Runtime comparison (min.)



- Order of magnitude increase in runtimes from $N-2$ to $N-1-1$
- Scalability is an issue (PSIP for each time-period pairs)

Preliminary Observations (3 of 3)

- detailed relations between $N-2$ and $N-1-1$?
- Need more comprehensive studies on larger (and more realistic) systems to draw conclusion

Current and Next Steps

- Model refinements
 - enforcing non-anticipativity between primary and secondary contingency
- Algorithmic refinements
 - HPC implementation
- Further testing and analysis
 - Larger and more realistic instances
 - Longer time periods (e.g. $T = 8, 12, 24$)
 - Rolling horizons
 - $N-2$ and $N-1-1$?

Thank you

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