

# Value of Modelling Constraints in Generation Scheduling

## Towards Computationally Efficient Scheduling Proxies

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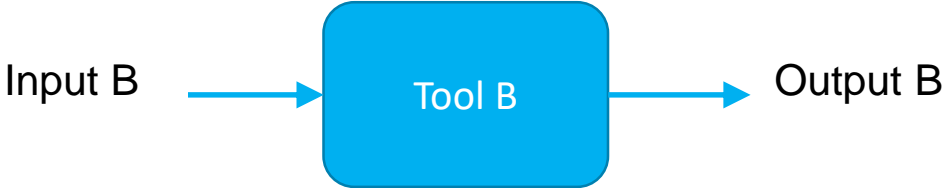
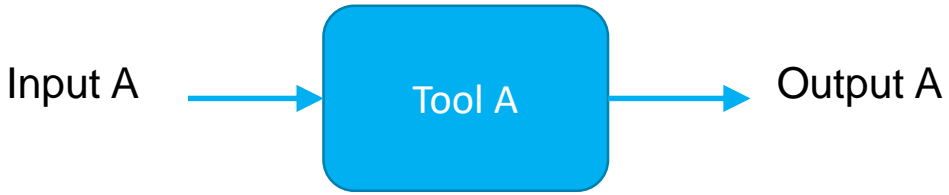
FERC Software Conference  
June 26<sup>th</sup>, 2019



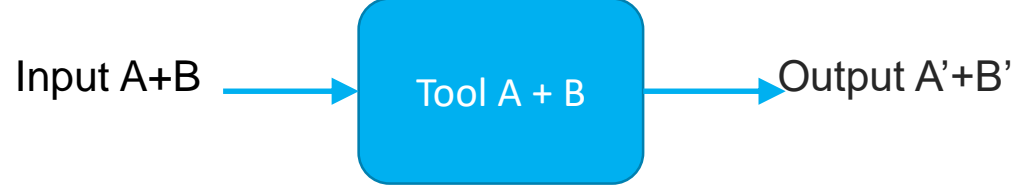
# Background: Link Power System Tools

- Problem:

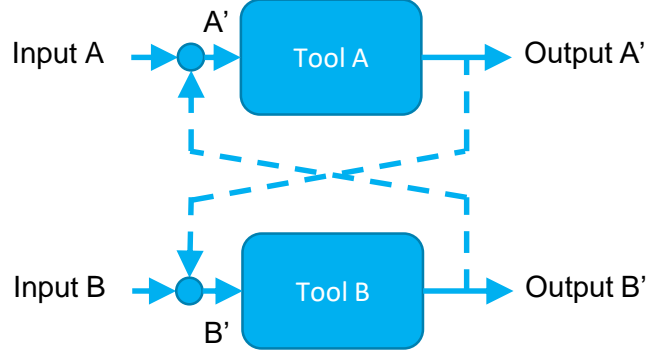
Two tools → two different domains:



- Single shot solution (Big computer!)



- Co-simulation



- Simplify the problem: Proxy

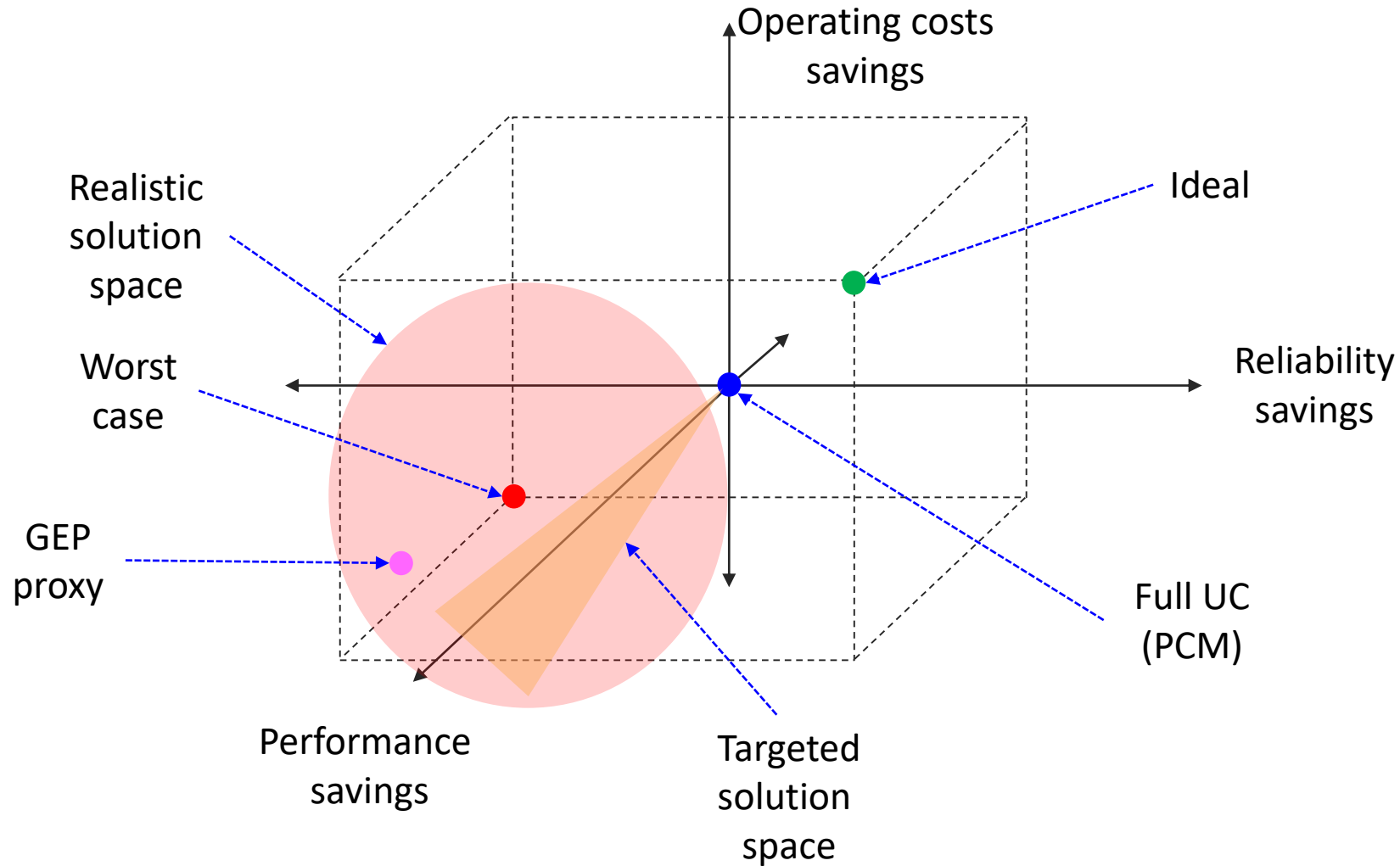


# Introduction

- Modeling accuracy in UC formulation increases computational burden
- Expansion tools need to explore long time horizons (20 years or more) and over multiple scenarios
- Expansion tools resort to simplified versions of UC (convolved LDCs, ignore binaries and constraints, temporal aggregation, cluster generation sets, among others)
  - Gain computational speed
  - Sacrifice solution accuracy
- Worked fairly well in the past, with “well-behaved” and predictable load patterns
- As the penetration of RES increases in the system, variability and uncertainty require greater degrees of flexibility
- The introduction of emerging technologies such as storage require modelling inter-temporal couplings

# Problem

- Find the tradeoffs between model accuracy and computational tractability



# Proposed Method



Step 1:  
Simplified UC

Speed up calculations

Modelling assumptions

Enforce desired constraint:

- a) Min. up & down times
- b) Reserves requirements
- c) Start-up costs
- d) Minimum stable generation ( $P_{\min}$ )
- e) Ramp rates



Step 2:  
Full UC formulation

**Fixed schedule** from Step 1

Enforce all UC constraints

Determine UC violations



Step 3:  
Cost and violations

Accommodate RT deviations

Determine dispatch and reserve violations

# Formulation

Full UC formulation:

$$\begin{aligned} & \min_{u,p} \left\{ \sum_{i \in I} c_i(u_{i,t}, p_{i,t}) \right\} \\ & L_t - p_t^{\text{RES}} - \sum_{i \in I} p_{i,t} = 0 \quad \forall t \in T \\ & u_i \cdot P_i^{\text{min}} \leq p_{i,t} \leq u_i \cdot P_i^{\text{max}} \quad \forall t \in T \\ & \mathbf{h}(\mathbf{u}, \mathbf{p}) \leq 0 \\ & u \in \{0, 1\} \\ & p \in \mathbb{R}^{0+} \end{aligned}$$

Simplified UC  
Variants

{Enforce  
some  
constraint(s)}

Most simplified generation  
“scheduling”:

$$\begin{aligned} & \min_p \left\{ \sum_{i \in I} c_i(p_{i,t}) \right\} \\ & L_t - p_t^{\text{RES}} - \sum_{i \in I} p_{i,t} = 0 \quad \forall t \in T \\ & 0 \leq p_{i,t} \leq P_i^{\text{max}} \quad \forall t \in T \\ & p \in \mathbb{R}^{0+} \end{aligned}$$

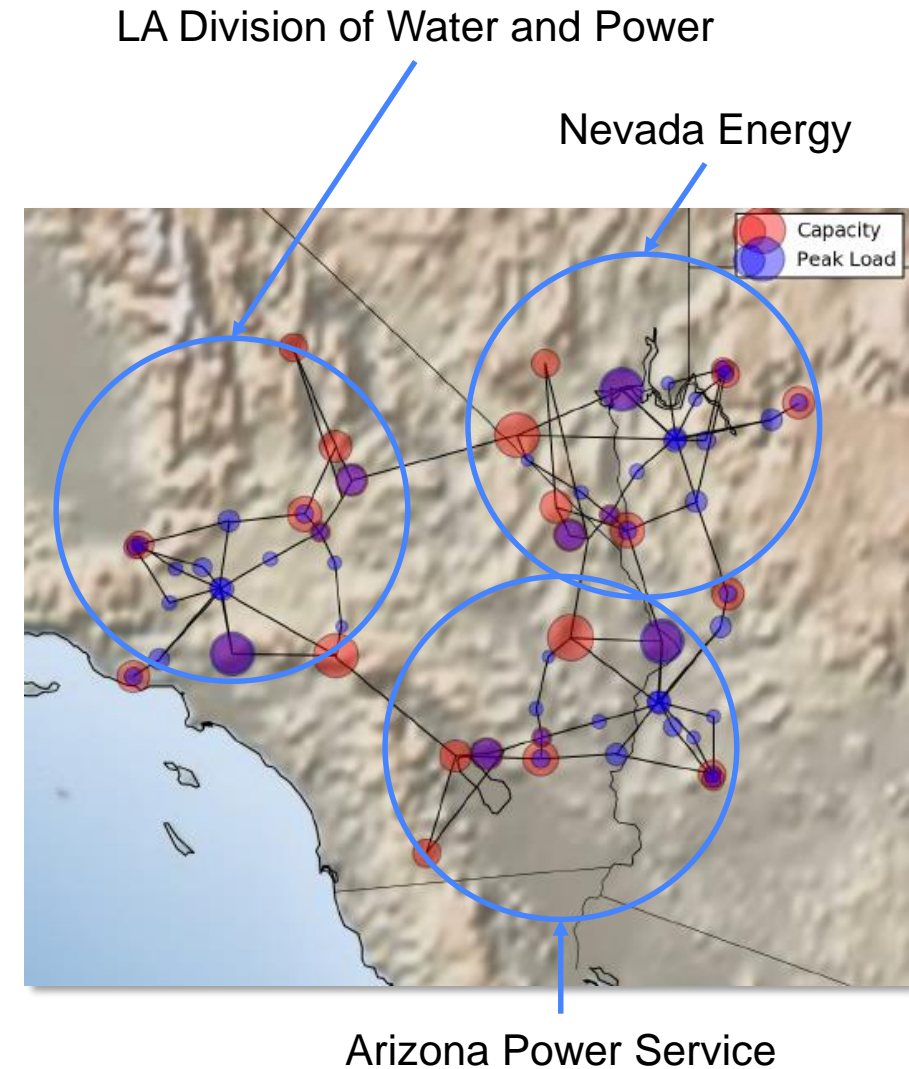
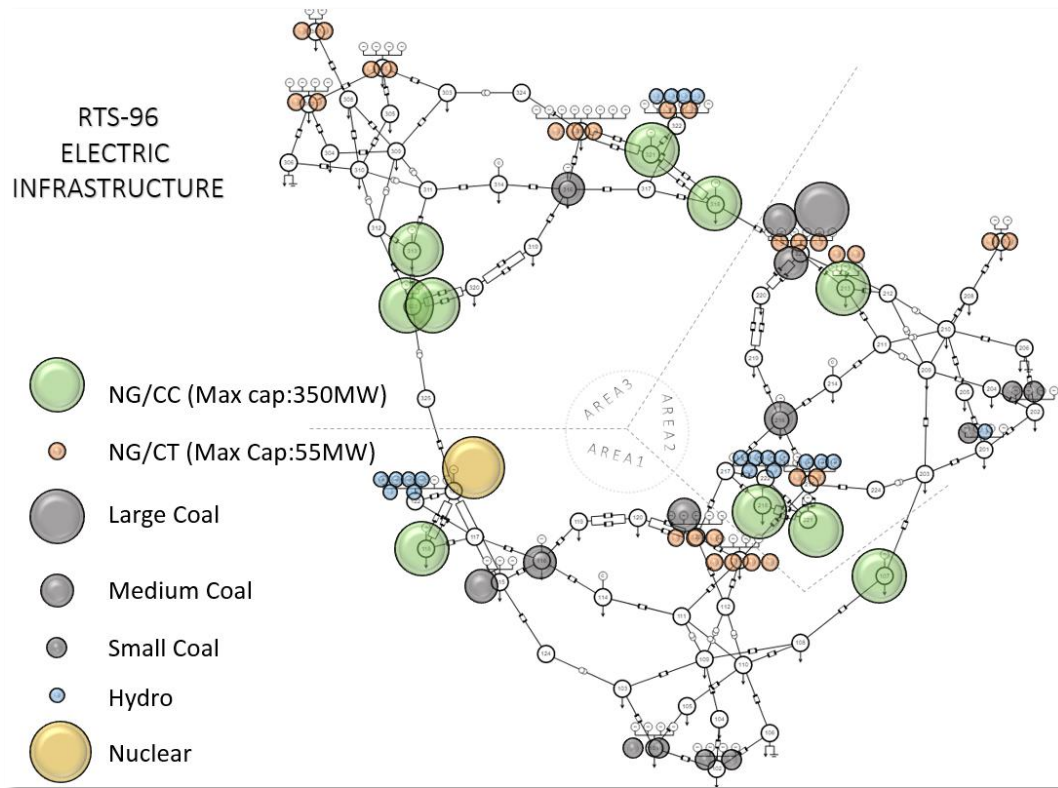
# Test Cases

- 1 Full UC model
- 2 Simplified UC: No min up&dn times; no reserves; no start-up; np Pmin; no ramps
- 3 UC enforcing units' minimum up and down times
- 4 UC enforcing system-wide reserve constraints
- 5 UC considering units' start-ups
- 6 UC enforcing generators' Pmin
- 7 UC enforcing generators' ramp rates



# Test System – RTS GMLC

- Adapted to represent three realistic area
- <https://github.com/GridMod/RTS-GMLC>





# Test System – RTS GMLC

| Generation type         | Number of units | Fuel        | P <sub>min</sub> (MW) | P <sub>max</sub> (MW) | Total (MW) | Ramp up (MW/min) | Ramp down (MW/min) |
|-------------------------|-----------------|-------------|-----------------------|-----------------------|------------|------------------|--------------------|
| Steam Turbine (ST)      | 7               | Oil         | 5                     | 12                    | 84.0       | 1                | 1                  |
| Combustion Turbine (CT) | 12              | Oli         | 8                     | 20                    | 240.0      | 3                | 3                  |
| Combustion Turbine (CT) | 27              | Natural Gas | 22                    | 55                    | 1458.0     | 3.7              | 3.7                |
| Steam Turbine (ST)      | 7               | Coal        | 30                    | 76                    | 532.0      | 2                | 2                  |
| Steam Turbine (ST)      | 7               | Coal        | 62                    | 155                   | 1085.0     | 3                | 3                  |
| Steam Turbine (ST)      | 2               | Coal        | 140                   | 350                   | 700.0      | 4                | 4                  |
| Combined cycle (CC)     | 10              | Natural Gas | 170                   | 355                   | 3550.0     | 4.14             | 4.14               |
| Nuclear                 | 1               | Nuclear     | 396                   | 400                   | 400.0      | 20               | 20                 |
| Hydro*                  | 20              | K water     | 0                     | 50                    | 400.0      | 0*               | 0*                 |
| Wind**                  | 4               | K wind      | --                    | --                    | 2507.9     | --               | --                 |
| Utility PV              | 25              | SI          | --                    | --                    | 1554.5     | --               | --                 |
| Rooftop PV              | 25              | SI          | --                    | --                    | 1161.4     | --               | --                 |

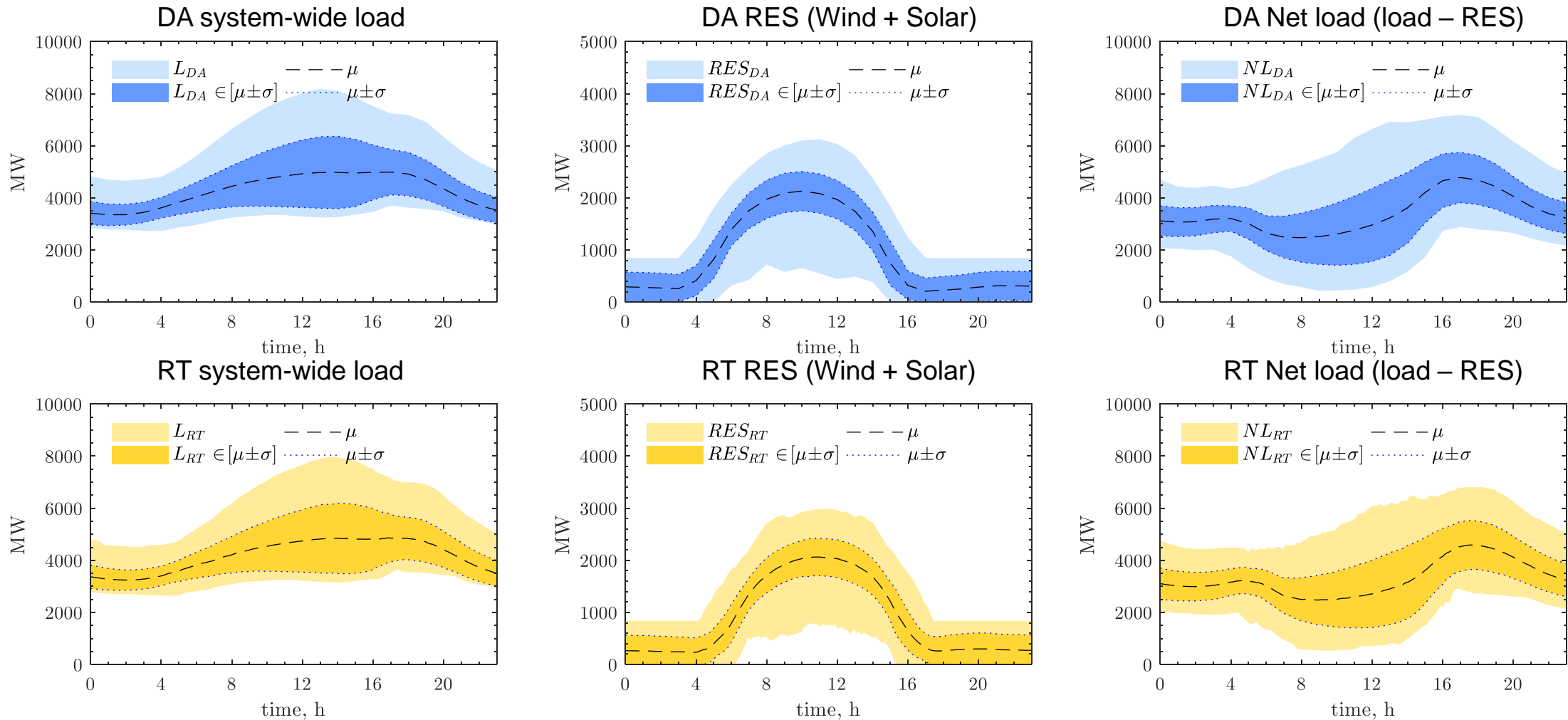
**Total = 13,672.8 MW**

\* Schedule determined by a hydro-thermal coordination and deemed as known for scheduling and dispatch purposes. This hydro profile data was obtained from [ref WECC TEPPC 2024]

\*\* Only one wind plan was modelled, 303\_WIND\_1

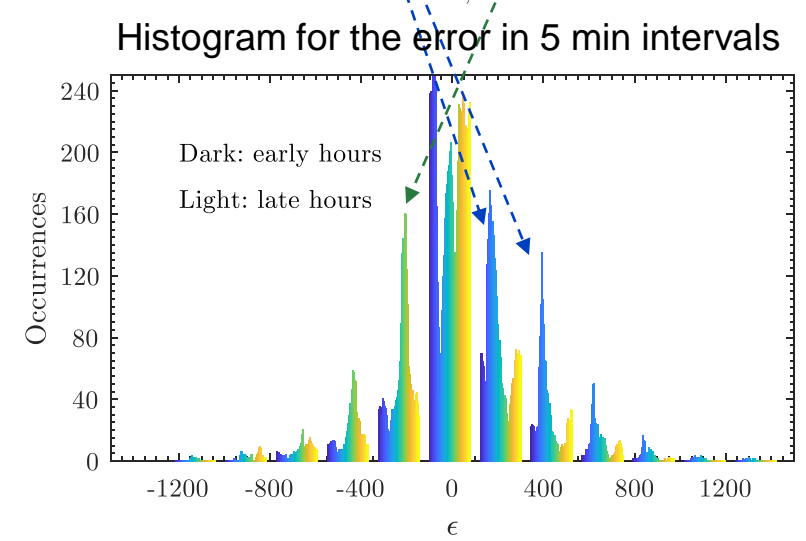
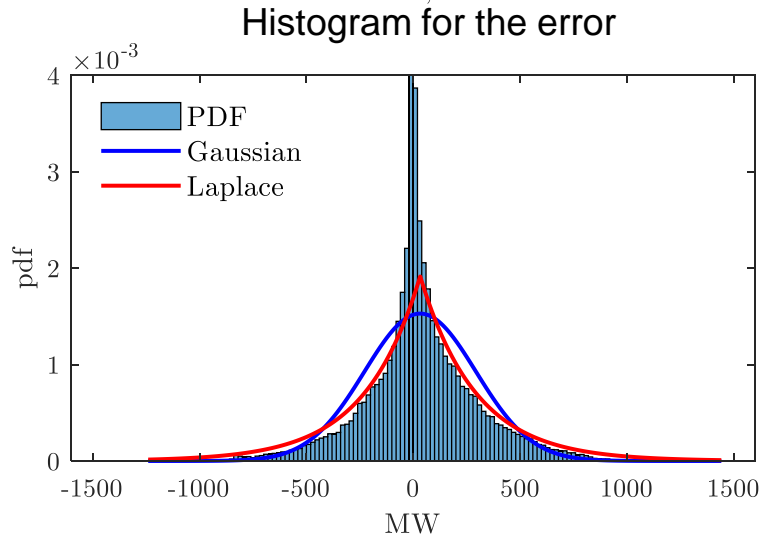
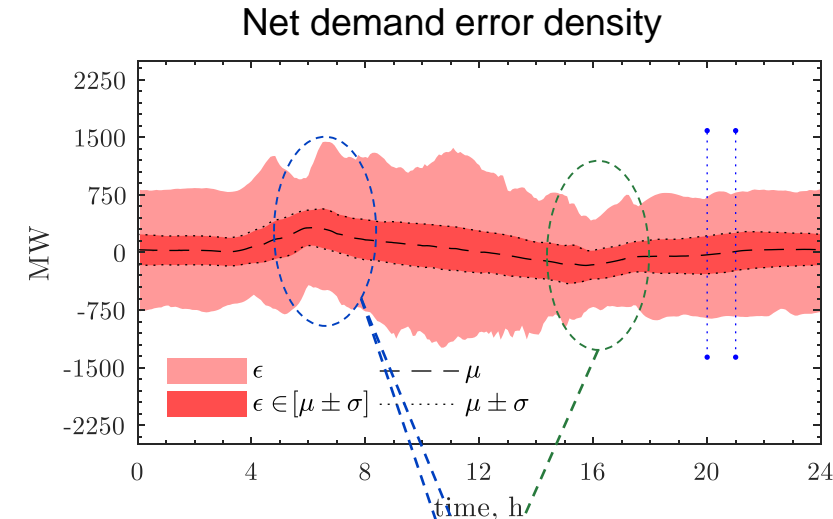
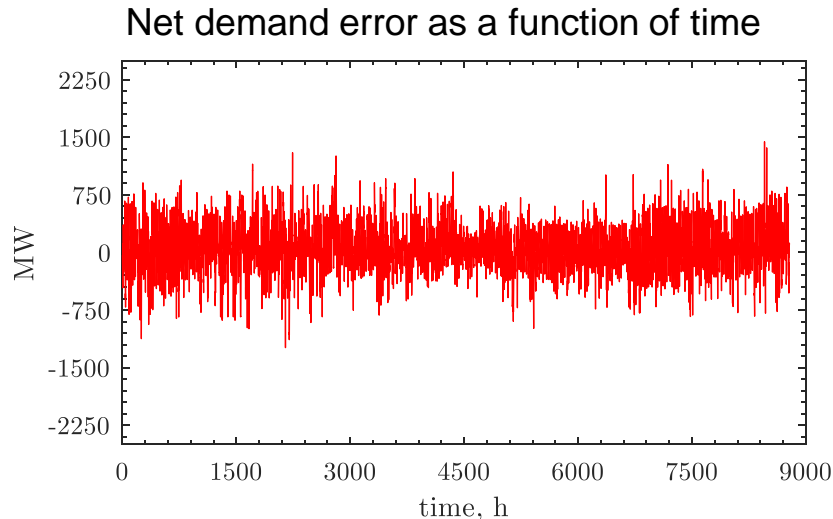
# Test System – RTS GMLC

- DA and RT time series (TS) for year 2020



# Test System – RTS GMLC's Net Demand Error

- Unavoidably, deviations from DA materialize in RT → System flexibility



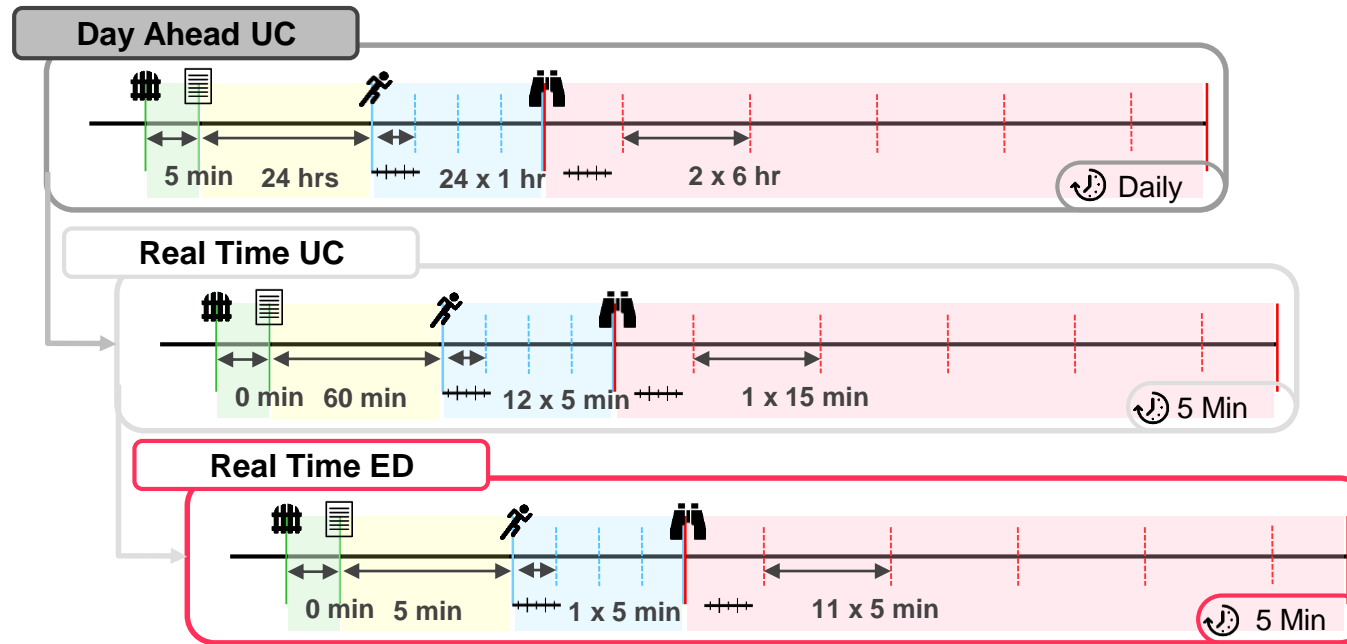
# Simulation Parameters

- Power System Optimizer (PSO) based on AIMMS
  - DA cycle: 24 h horizon with 1 h resolution. Nuclear unit is a must run
  - RT cycle: 1 h horizon with 5 min resolution. No additional synchronizations → dispatch only
- Reserve products from the RTS-GMLC (regulation, flexibility and spinning)
- Generator physical and operating limits, power balance, reserve requirements
- Penalty factors
  - Load balance violations: \$5000/MWh
  - Reserve violations: Regulation (\$1500/MWh); spinning (\$1250/MWh)
- Solution tolerances
  - MIP gap tolerance: 0.1% (DA and RT)
  - Time limit: 15 min. for DA and 5 min. for RT

<http://psopt.com/>

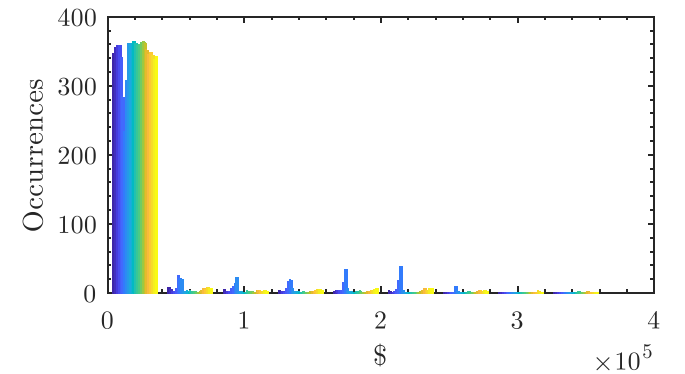
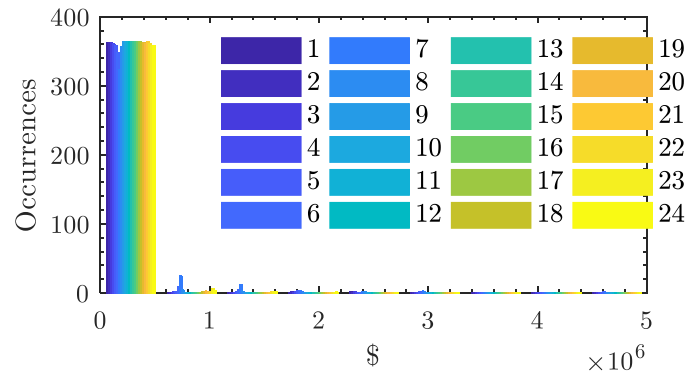
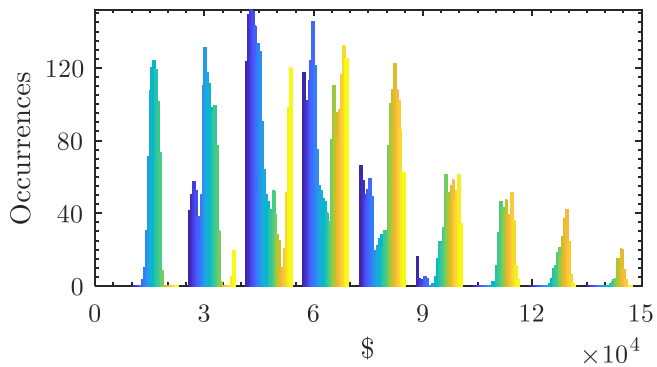
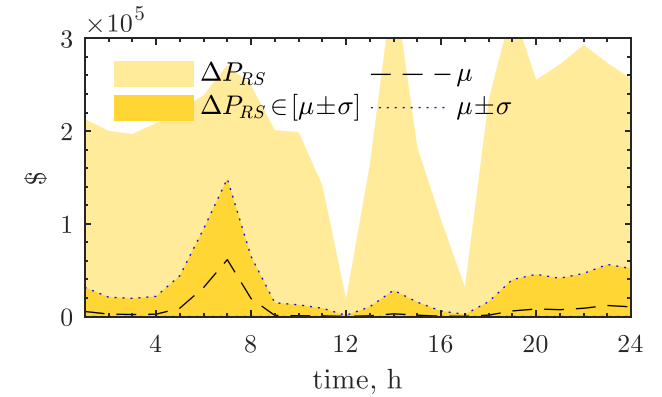
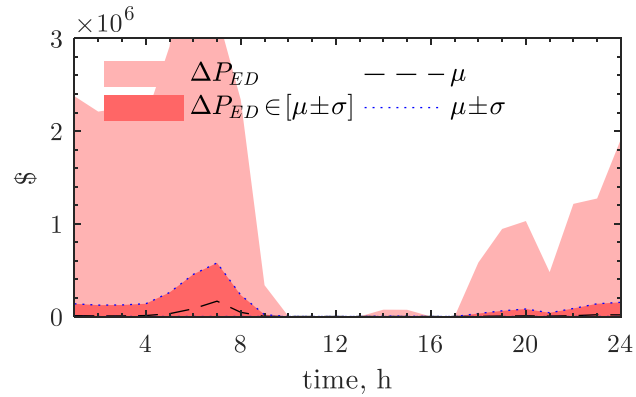
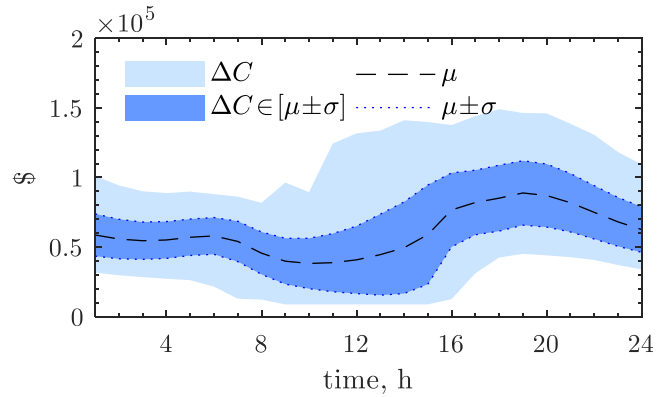
<https://github.com/GridMod/RTS-GMLC>

# Scheduling Process



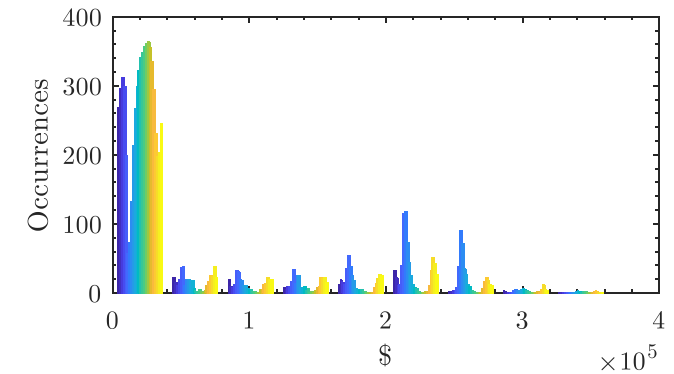
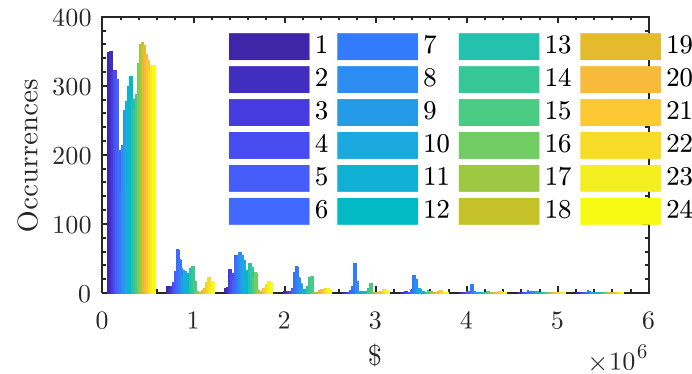
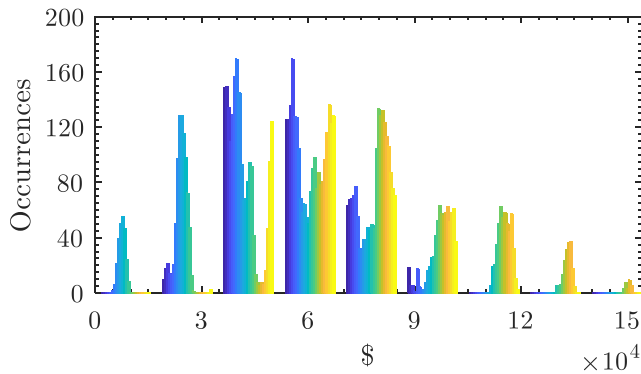
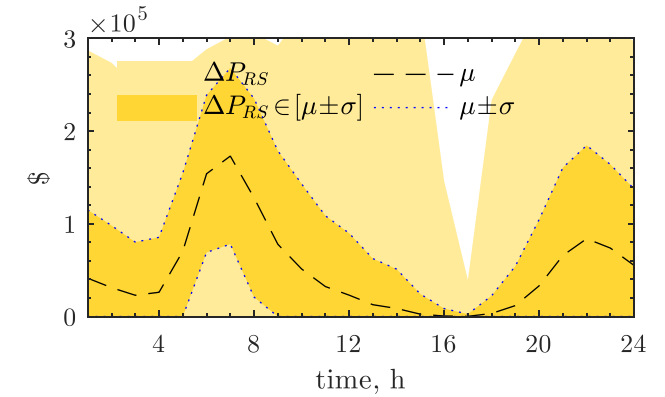
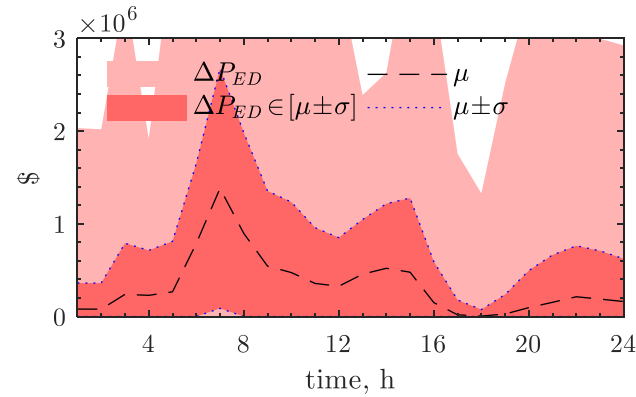
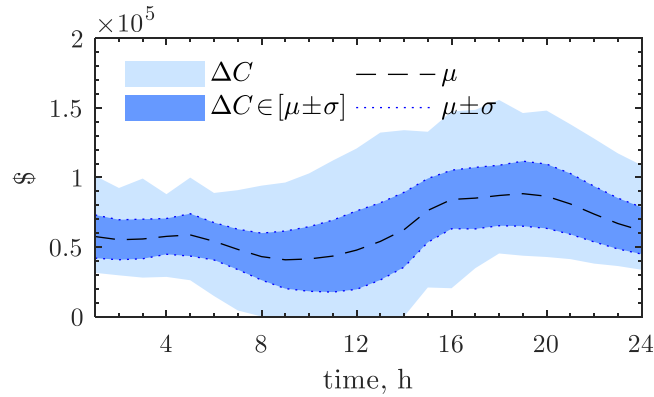
# Results

- Full UC formulation: operating costs; ED violations; and RS violations



# Results

- Simplified UC formulation: operating costs; ED violations; and RS violations





# Results

- Results are normalized with respect to the simplified UC

Simplified UC:

Solve time: 613.4 s (>10 min)

Cost: M\$ 548.22

UC penalties: M\$ 6,371.83

ED penalties: M\$ 2,949.75

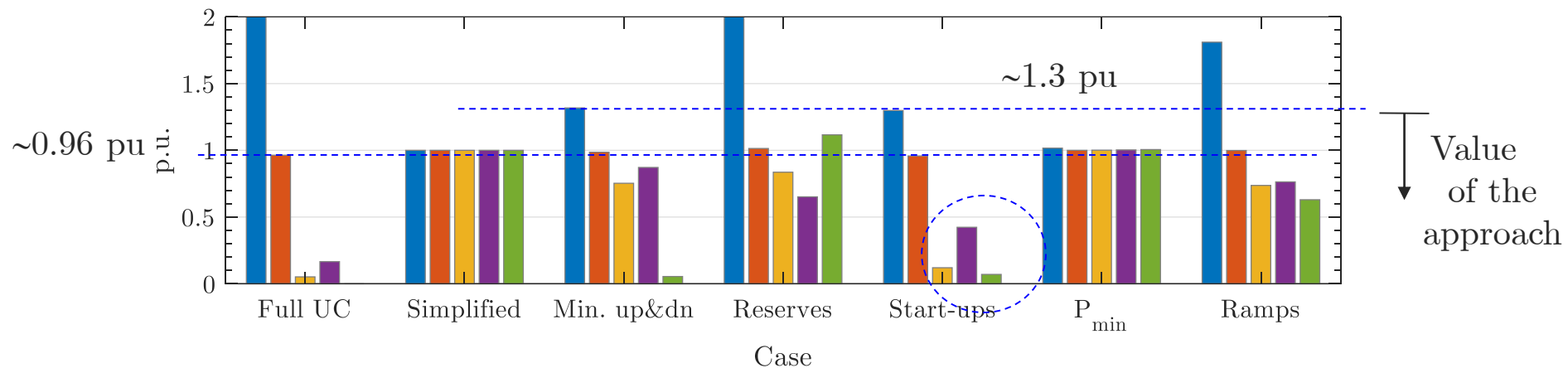
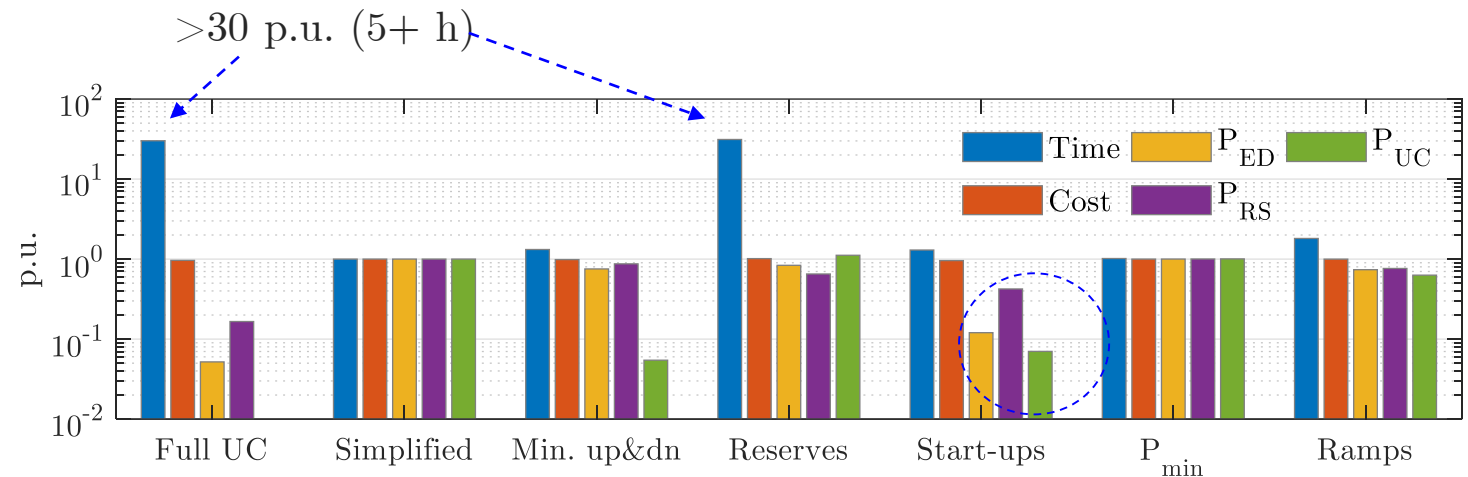
RS penalties: M\$ 429.39

Gap:  $1 \times 10^{-3}$

Intel Xeon CPU E5-2643

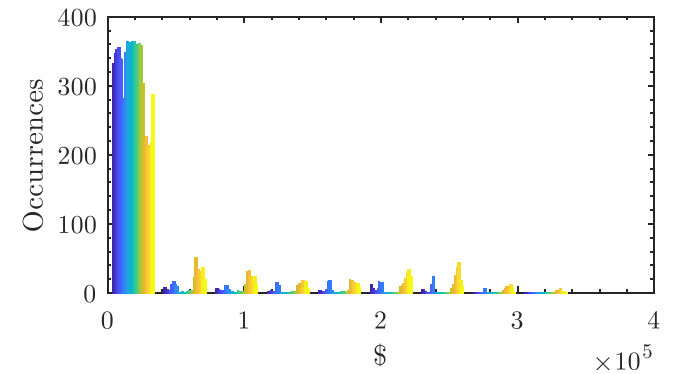
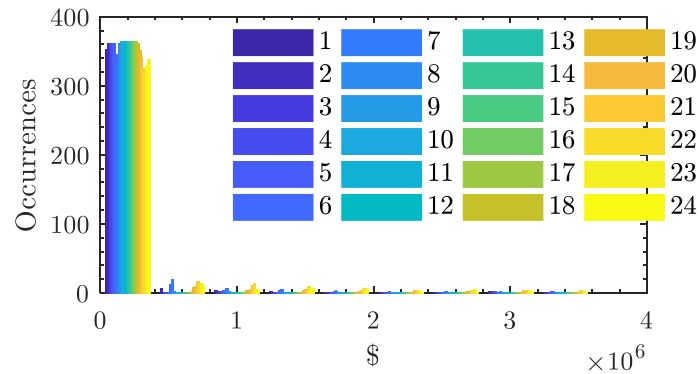
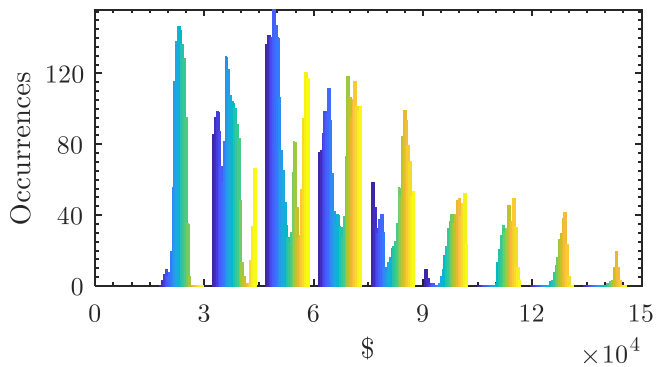
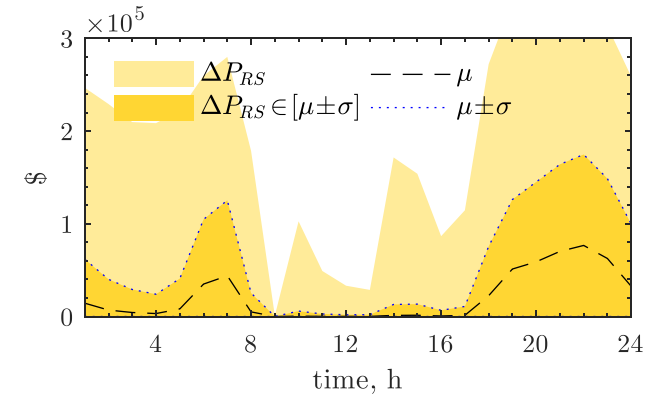
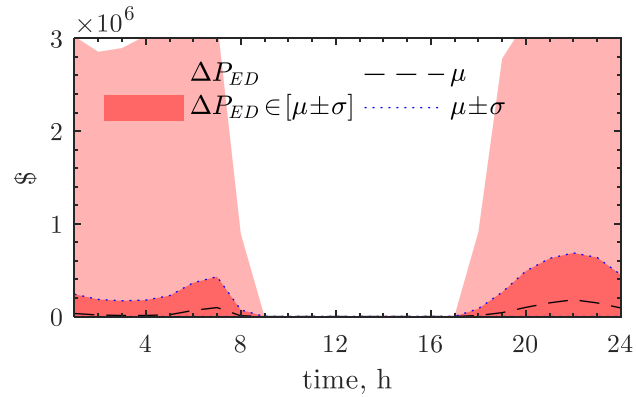
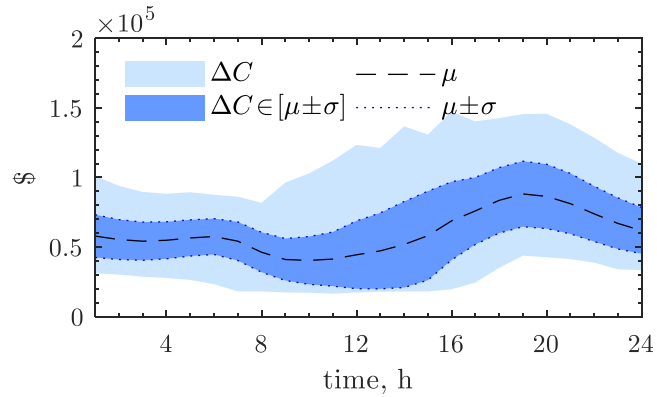
3.40 GHz (2 processors)

96 GB RAM

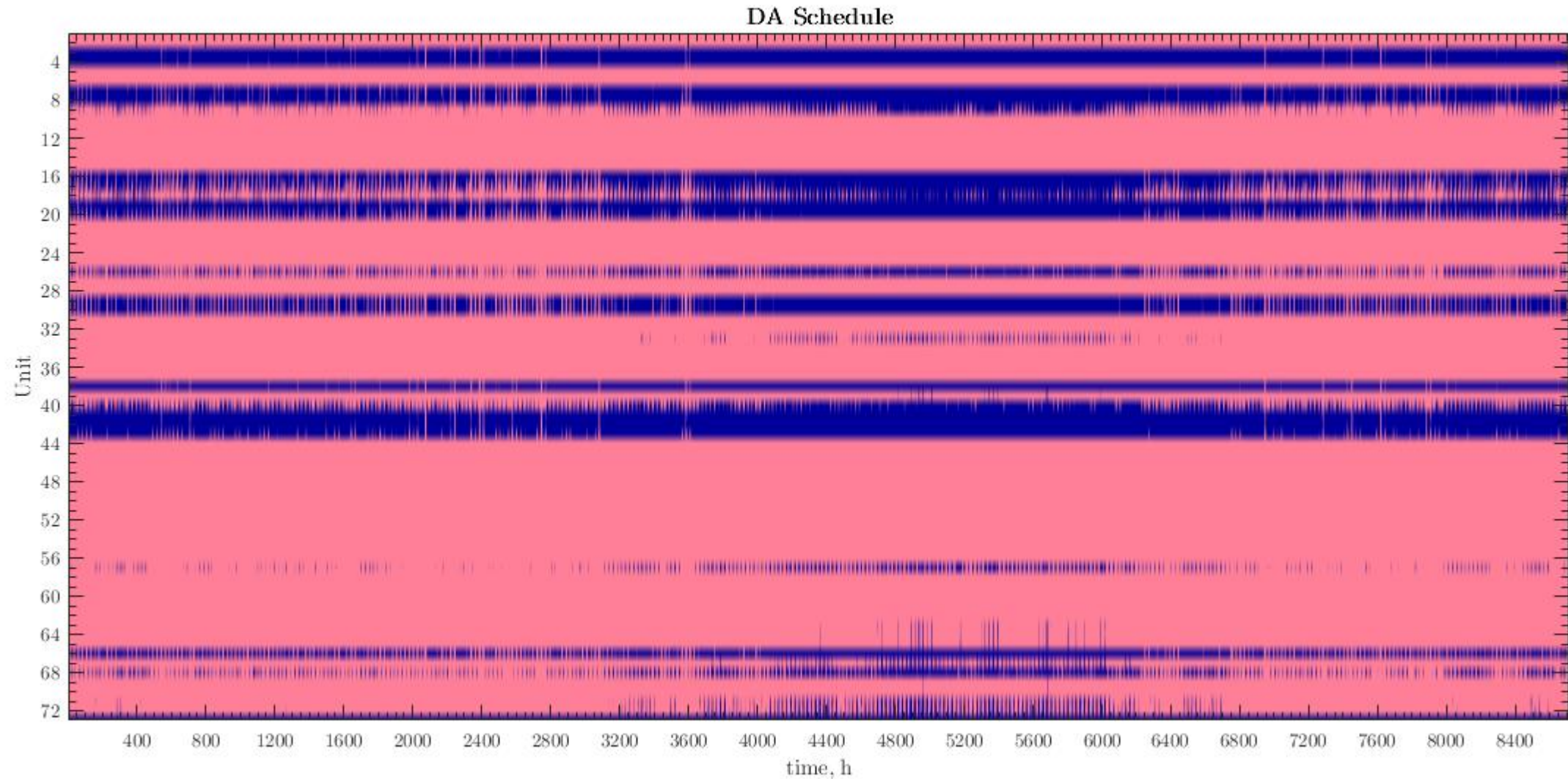


# Results

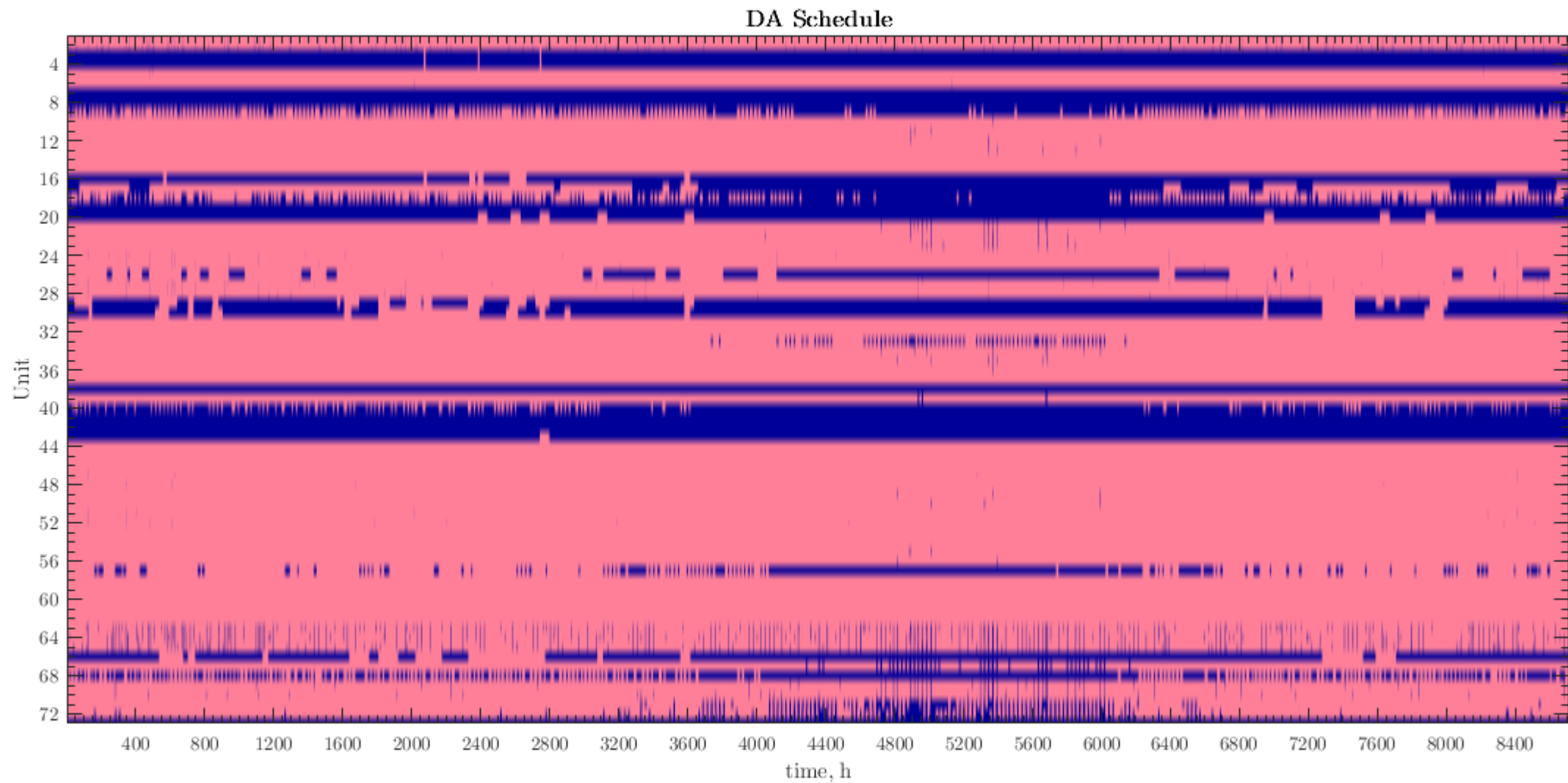
- Modeling start-up costs only



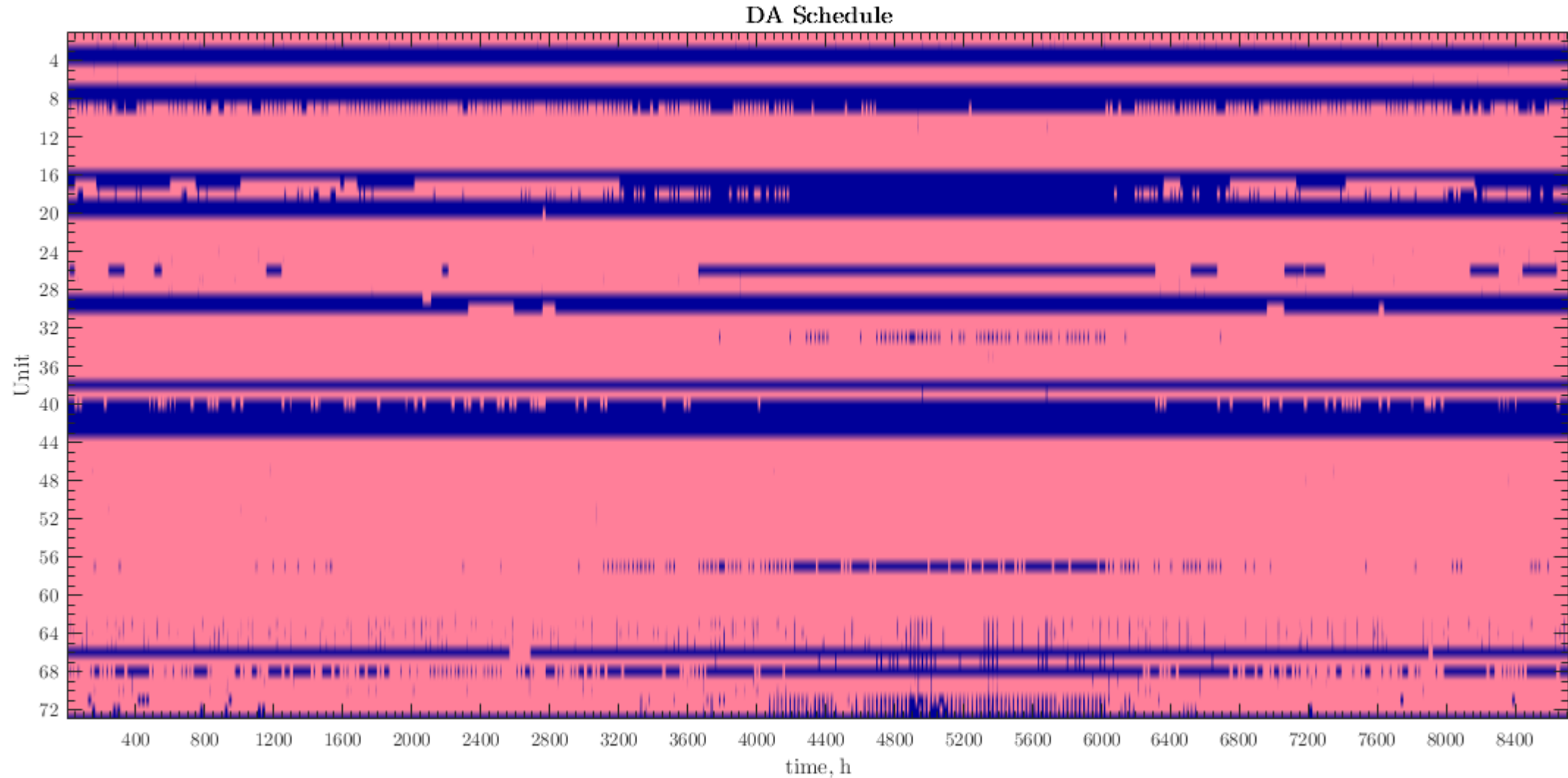
# Unit Commitment – Simplified UC



# Unit Commitment – Full UC

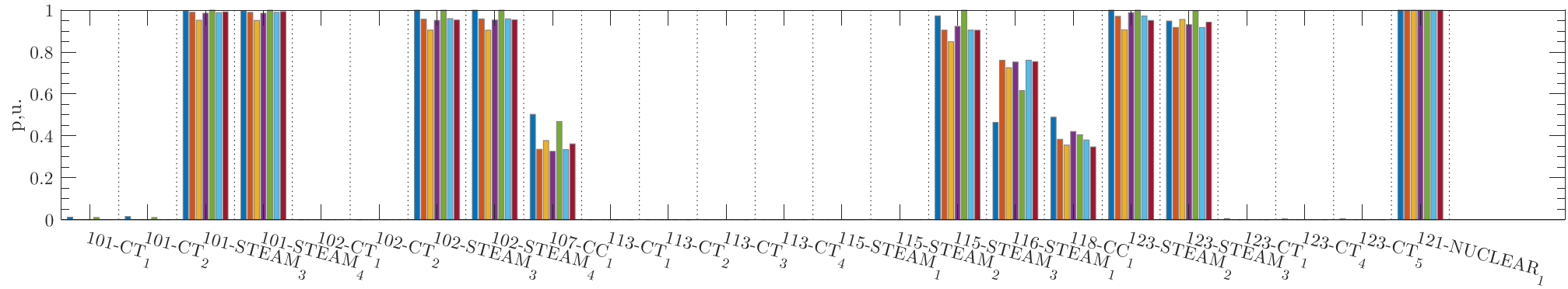


# Unit Commitment – Start-ups Only

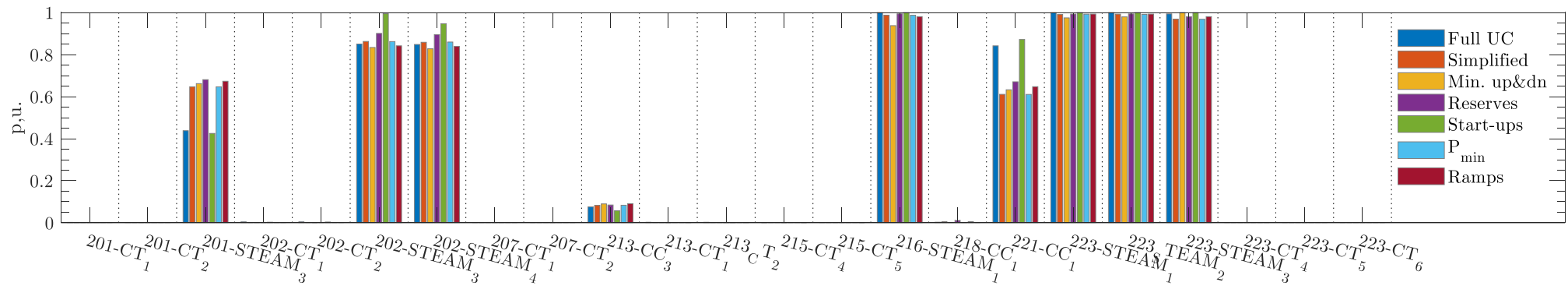


# Units' Utilization – Normalized Hours Committed

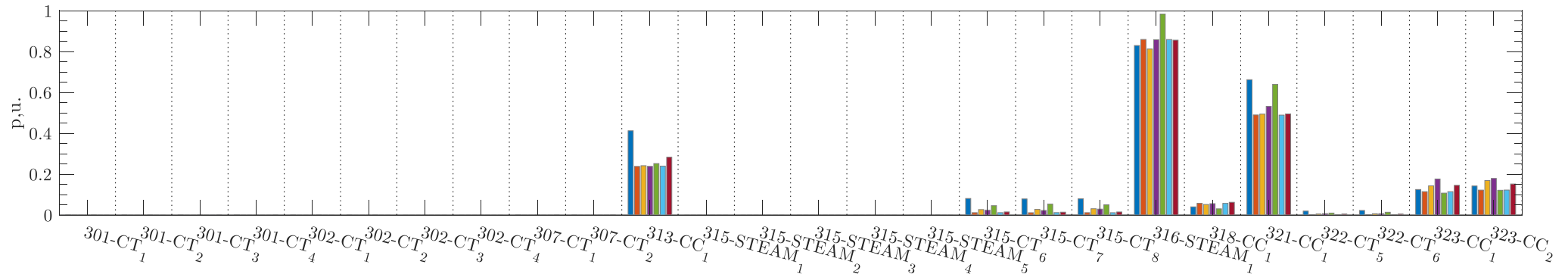
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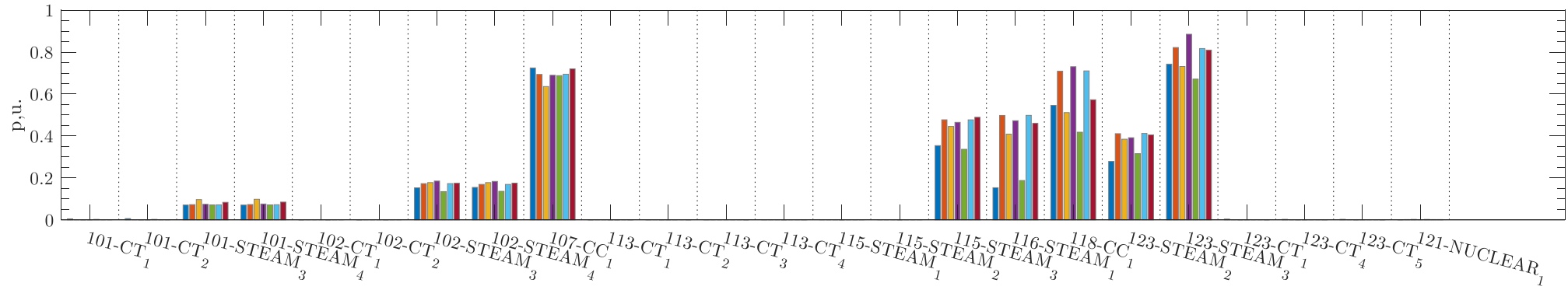


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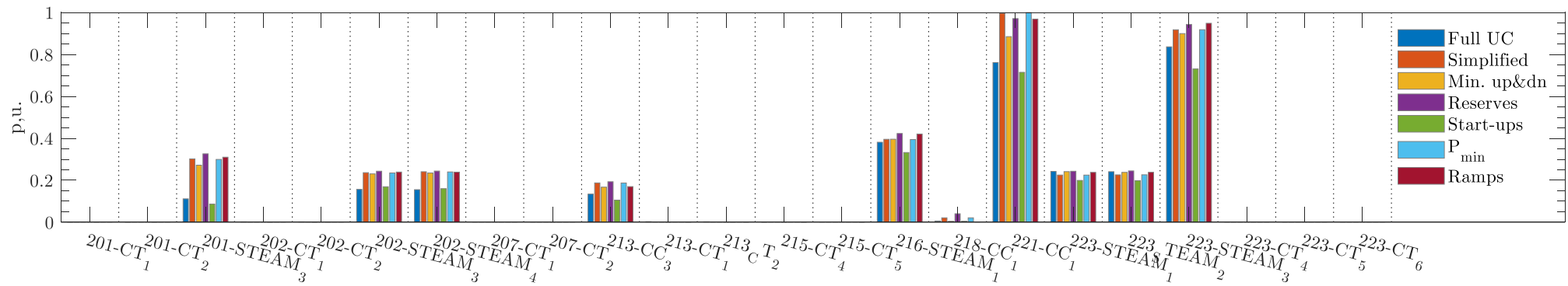


# Units' Utilization – Normalized Units' Mileage

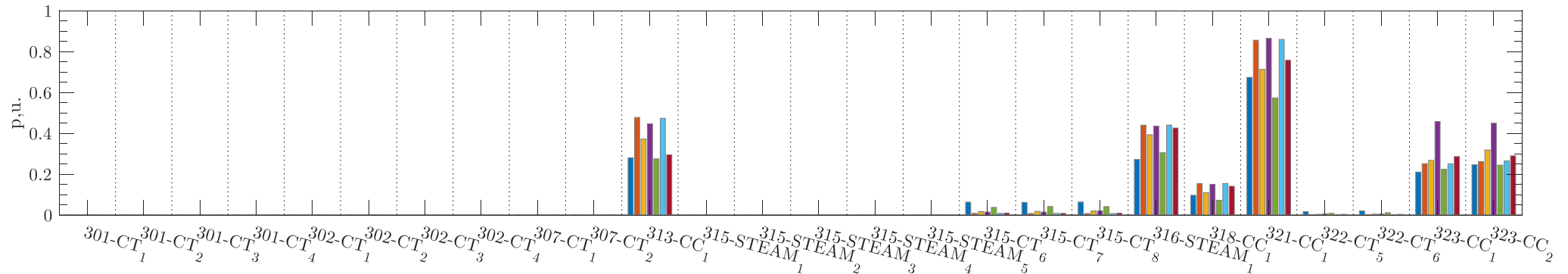
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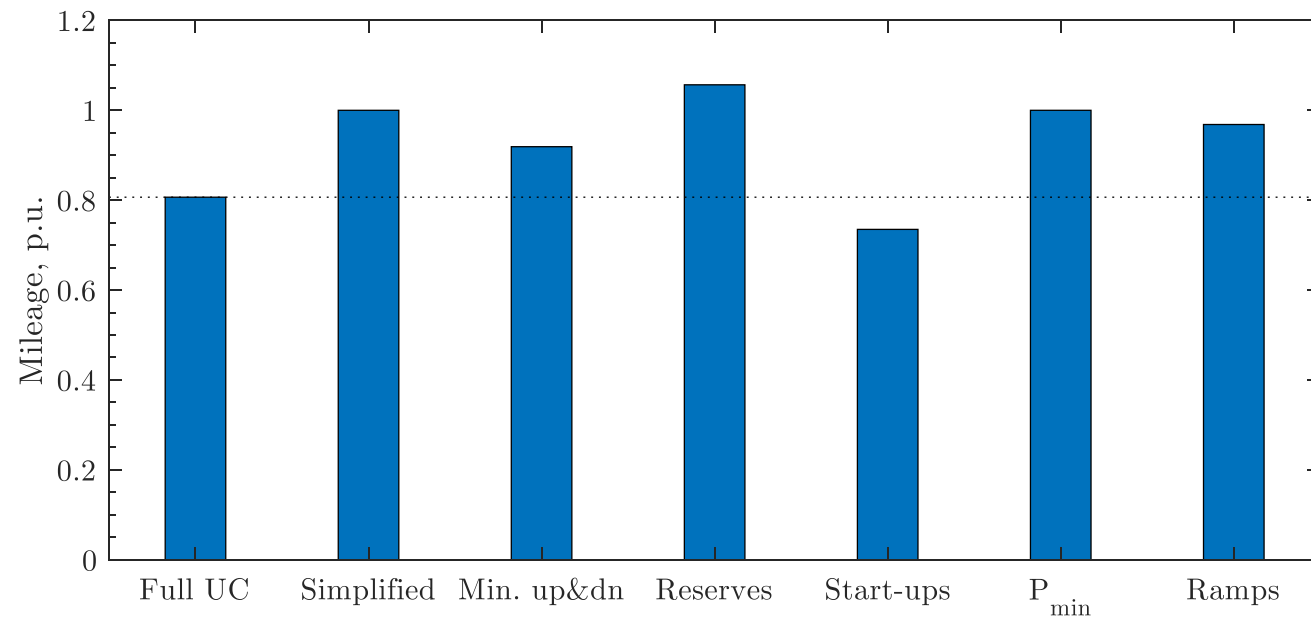
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# Aggregated Mileage

- Net demand mileage is the same regardless of the generation schedule
- Each approach results in different aggregated system mileage and cycling



# Aggregated Mileage

- Net demand mileage is the same regardless of the generation schedule
- Each approach results in different aggregated system mileage and cycling
- Example: Assume 2 units with start-ups cost costs of \$ 25, and the data on the tables below:

Generators

|        | $P_{\min}$<br>MW | $P_{\max}$<br>MW | $\pi$<br>\$/MWh |
|--------|------------------|------------------|-----------------|
| Unit 1 | 10               | 100              | 1               |
| Unit 2 | 10               | 100              | 2               |

Load

| Load     | $t_1$ | $t_2$ | $t_3$ |
|----------|-------|-------|-------|
| Forecast | 110   | 100   | 110   |
| Actual   | 100   | 100   | 100   |

Scheduling cases:

- Ignore start-up costs
- Consider start-up costs

UC&ED "a"

|        | $t_1$ | $t_2$ | $t_3$ |
|--------|-------|-------|-------|
| Unit 1 | 90    | 100   | 90    |
| Unit 2 | 10    | -     | 10    |

Cycling "a"

|        | $ \Delta t_{21} $ | $ \Delta t_{32} $ |
|--------|-------------------|-------------------|
| Unit 1 | 10                | 10                |
| Unit 2 | 10                | 10                |

UC&ED "b"

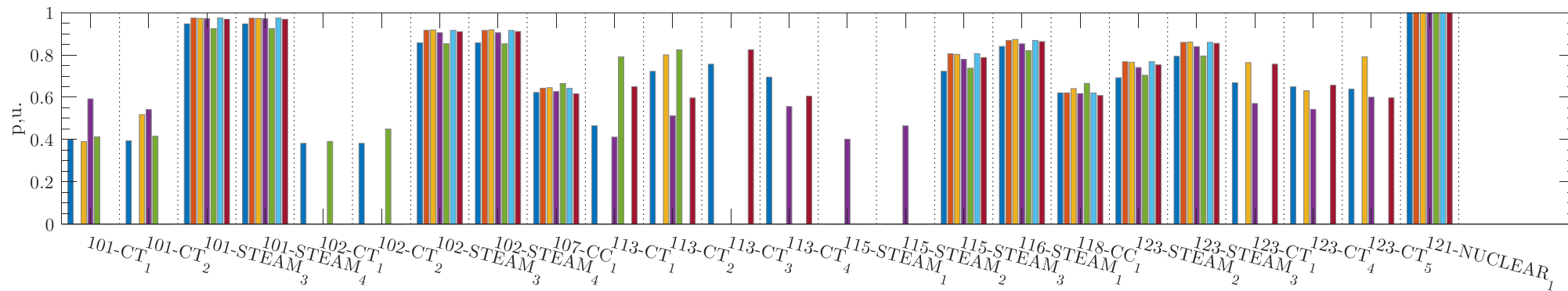
|        | $t_1$ | $t_2$ | $t_3$ |
|--------|-------|-------|-------|
| Unit 1 | 90    | 90    | 90    |
| Unit 2 | 10    | 10    | 10    |

Cycling "b"

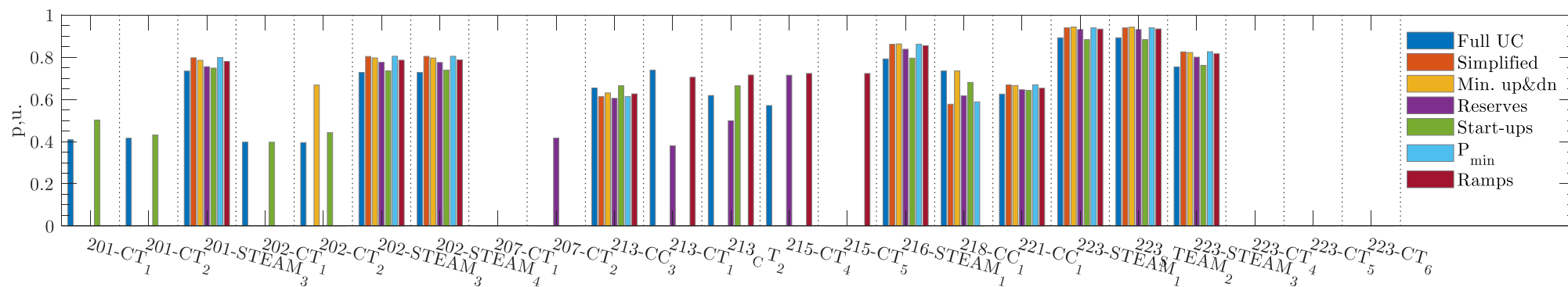
|        | $ \Delta t_{21} $ | $ \Delta t_{32} $ |
|--------|-------------------|-------------------|
| Unit 1 | 0                 | 0                 |
| Unit 2 | 0                 | 0                 |

# Units' Utilization – Units' Utilization Factor

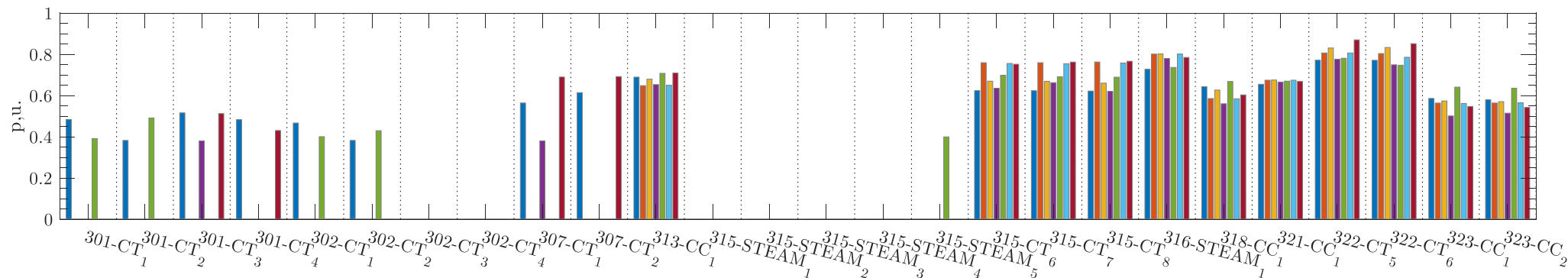
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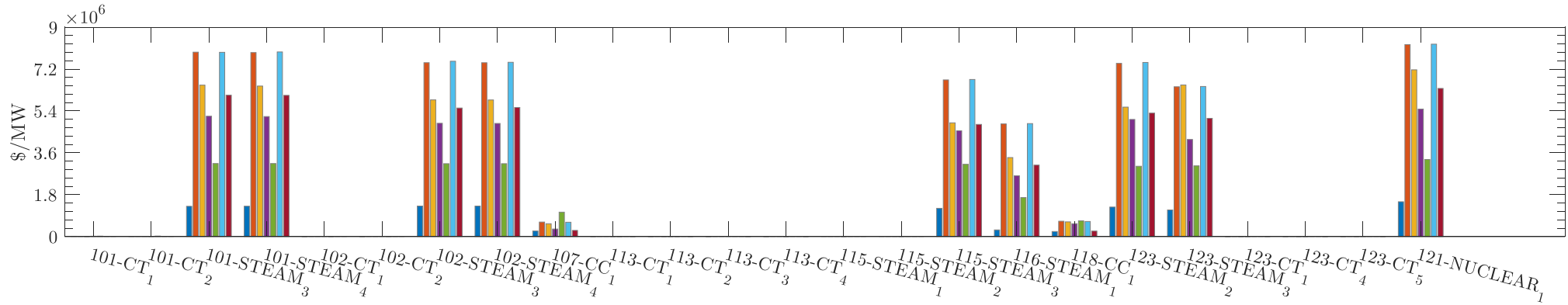


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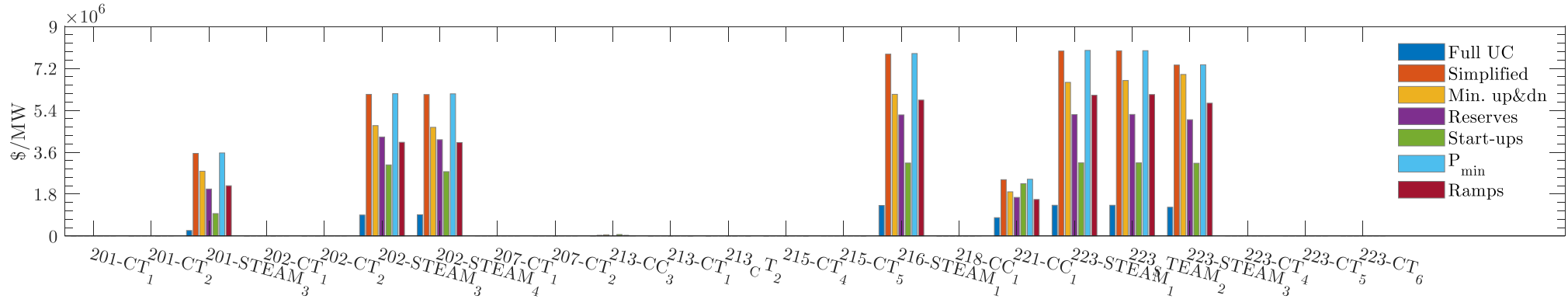


# Units' Profits

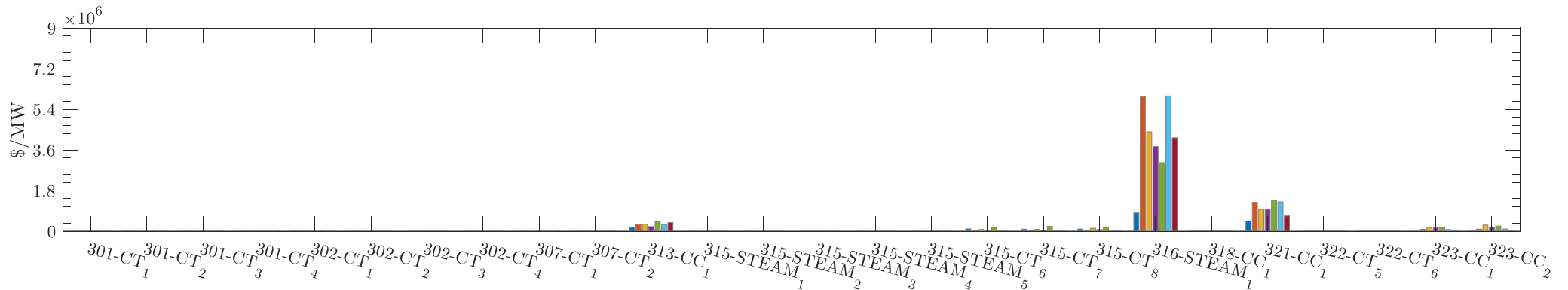
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# Conclusions

- Enforcing start-ups serves as an **indirect umbrella** for other constraints:
  - Min. up & down times:
    - Once a unit is synchronized/shut-down, it will remain as “long” as possible to avoid additional start-up costs
    - These on/off periods exceed the minimum up and down times
  - Ramps:
    - Optimization is performed over a time horizon. Keeping sufficient generation synchronized/offline considering the implicit look-ahead periods avoids unnecessary ramping
  - Minimum stable generation ( $P_{\min}$ ):
    - Synchronized generation is used to meet demand considering look-ahead periods, and since its synchronization comes at a cost, unnecessary generation is not synchronized and online generation is dispatched above  $P^{\min}$ .
  - Reserves:
    - Optimization is performed over long horizons where net demand varies. In order to keep costs at a minimum, sufficient capacity is kept to meet expected peak periods. During lower net demand periods there is an implicit generation margin, i.e. reserve.

# Conclusions

- Important to avoid over-generalizations
- Determine sensitivity of start-ups to different parameters
  - Fuel and carbon costs
  - Different penetrations of RES
- Pave the way to new array of tools at EPRI
  - Able to simulate and solve multiple scenarios → contingency screening and risk planning
  - New family of expansion tools that account for operating needs

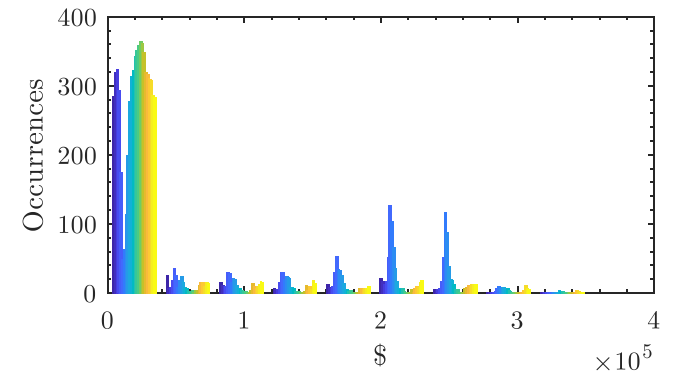
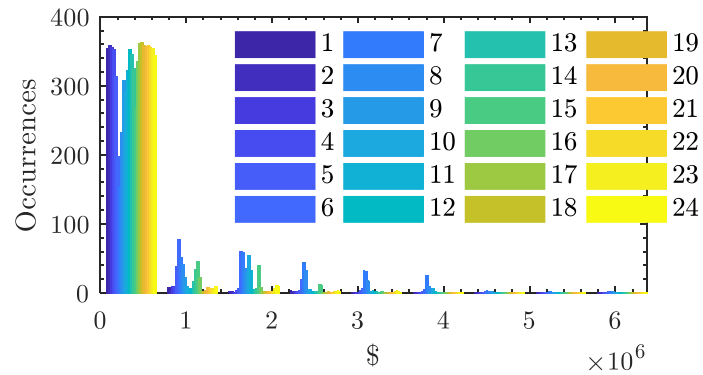
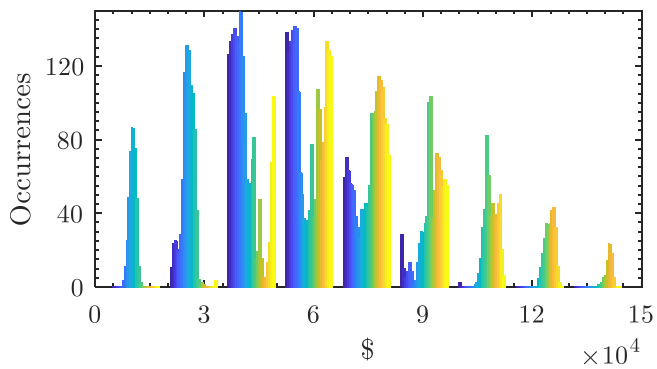
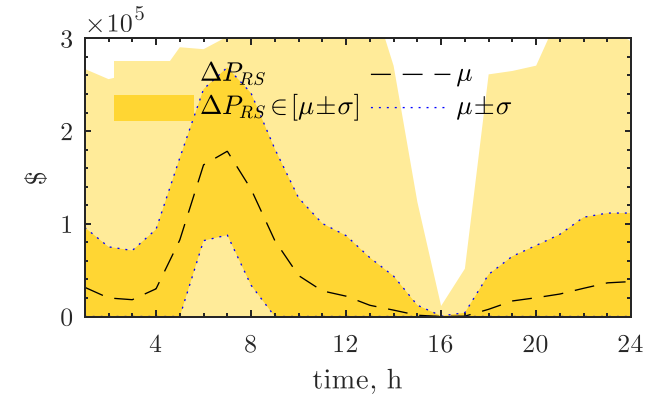
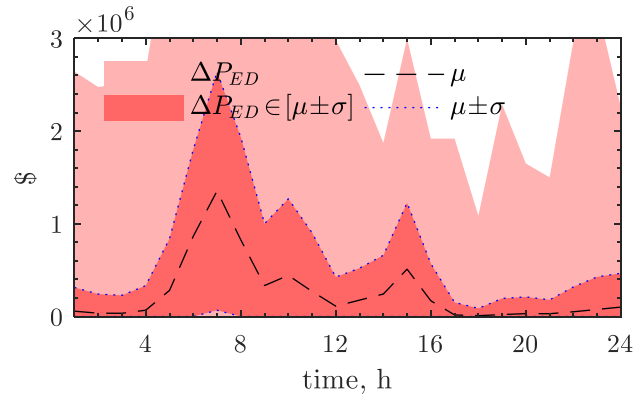
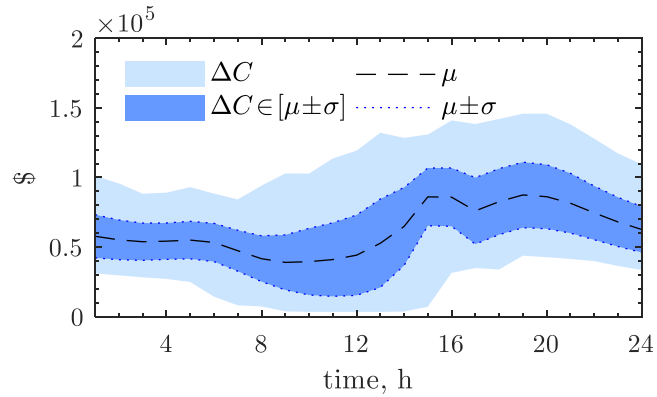
# Together...Shaping the Future of Electricity



# Support material

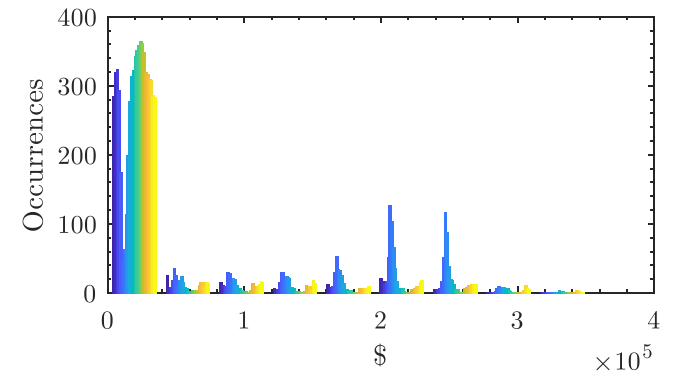
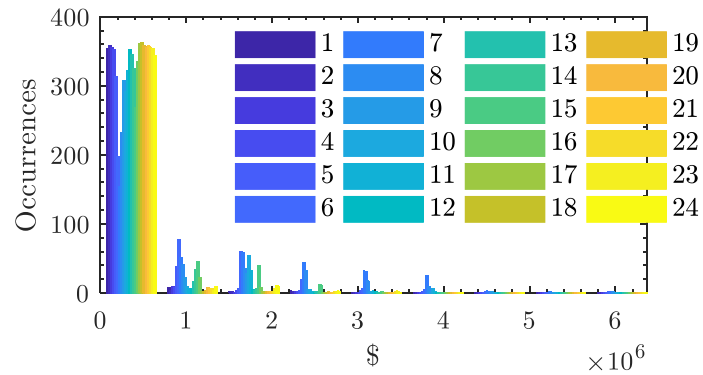
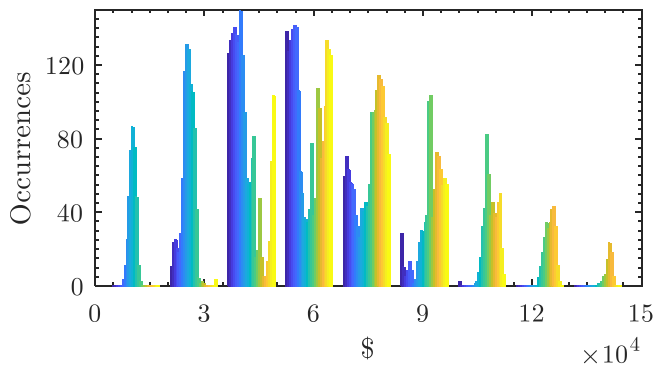
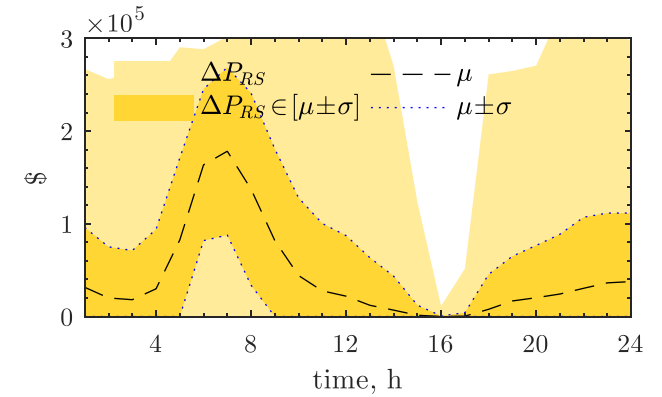
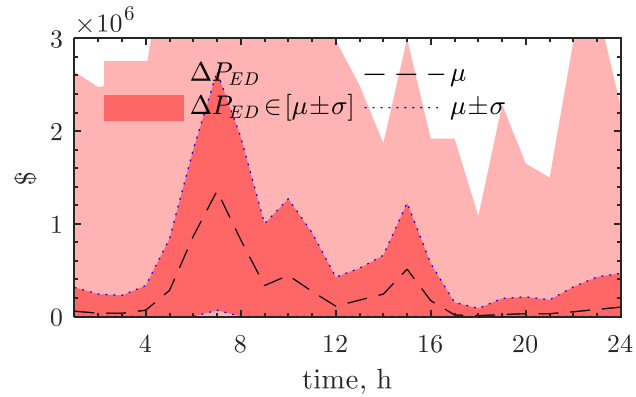
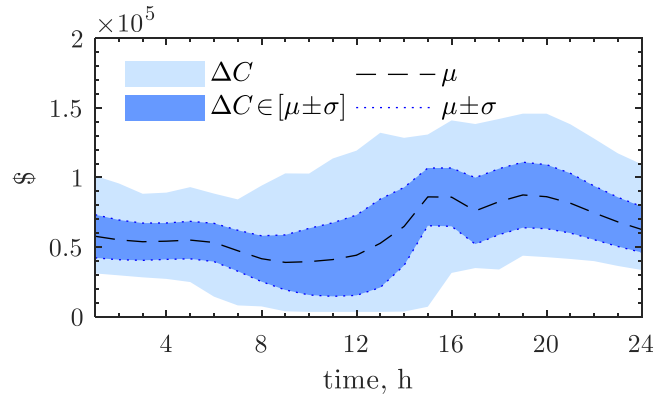
# Results

## Modeling minimum up and down times



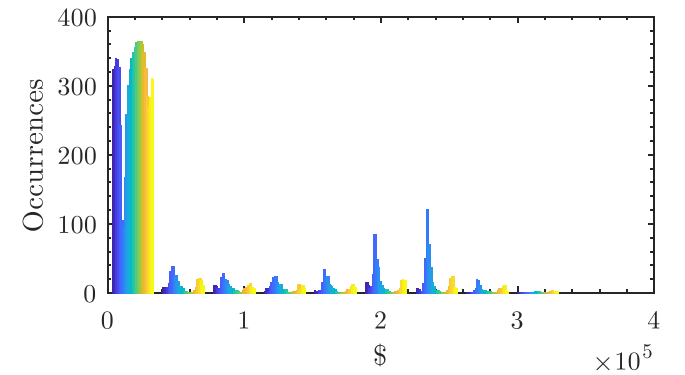
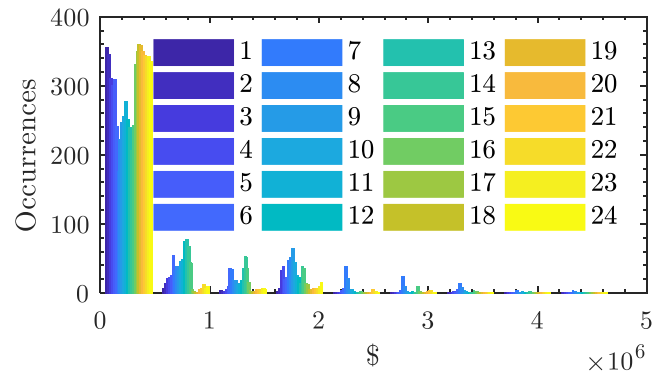
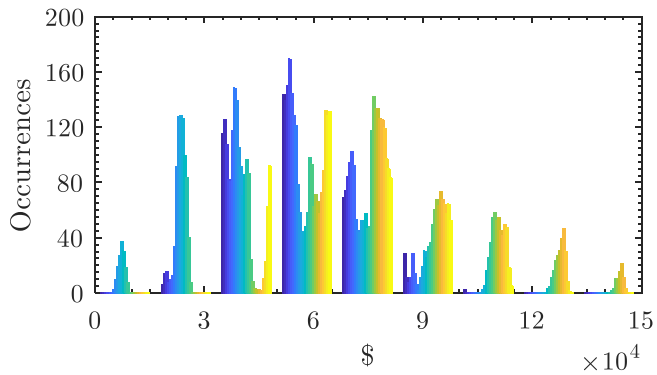
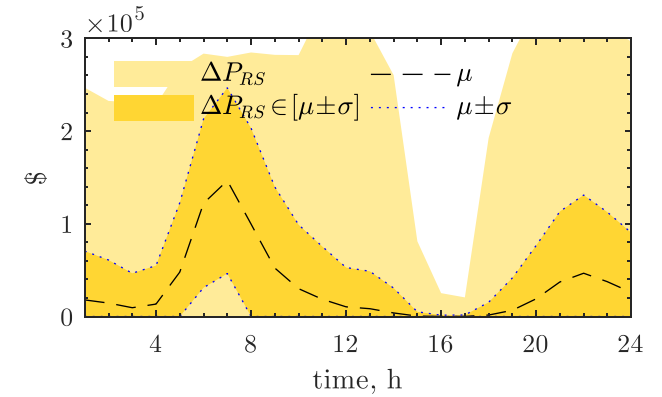
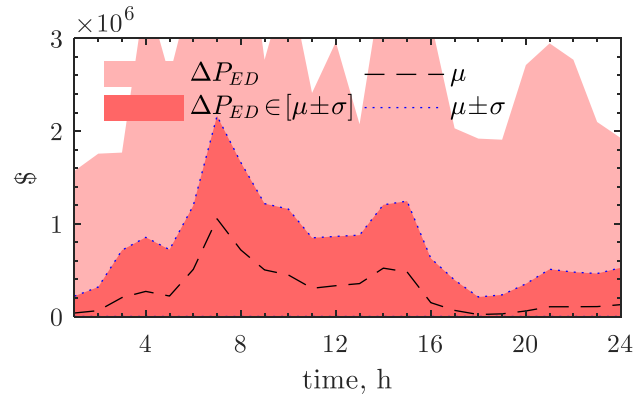
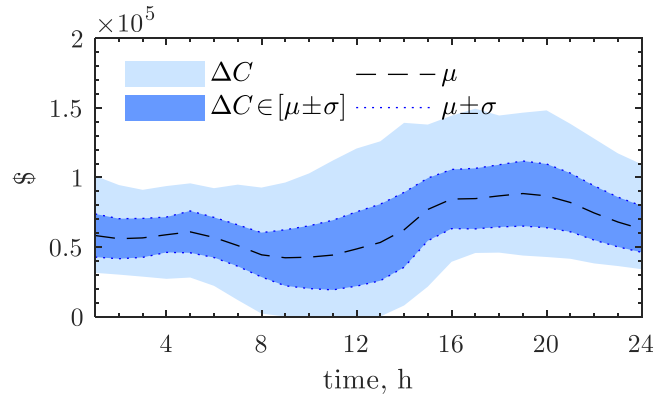
# Results

- Modeling minimum up and down times only



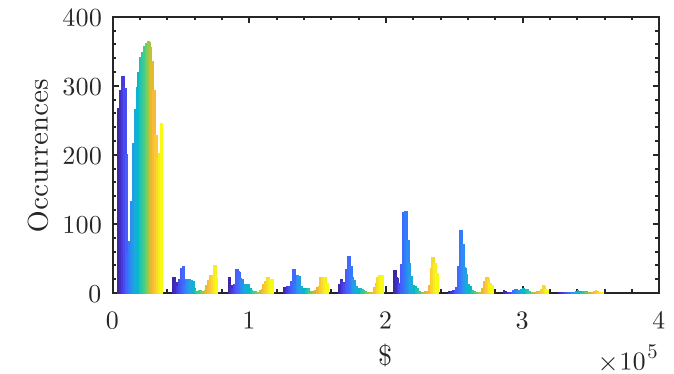
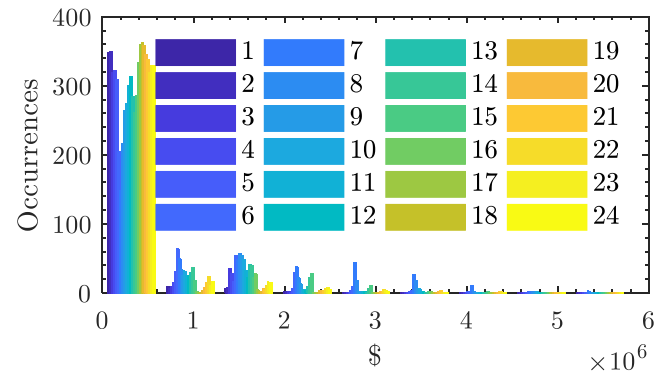
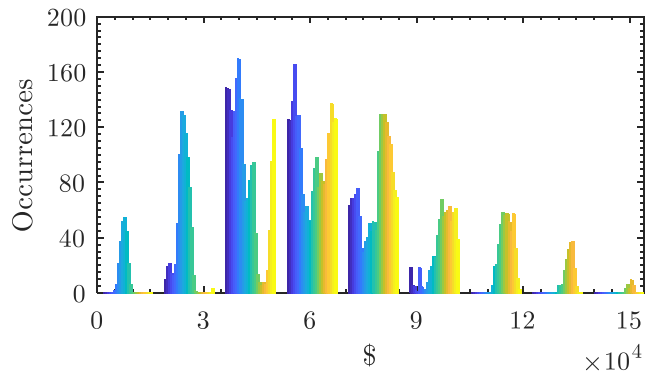
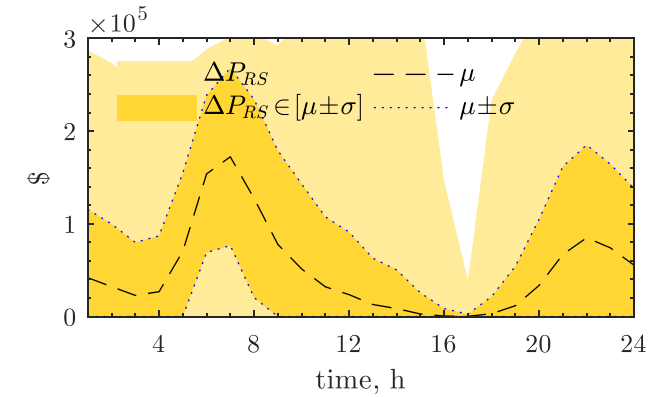
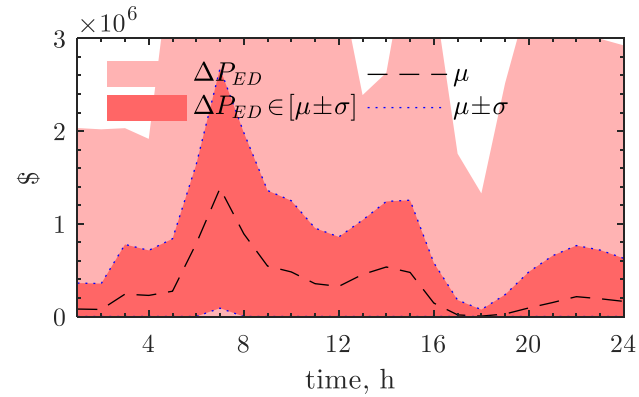
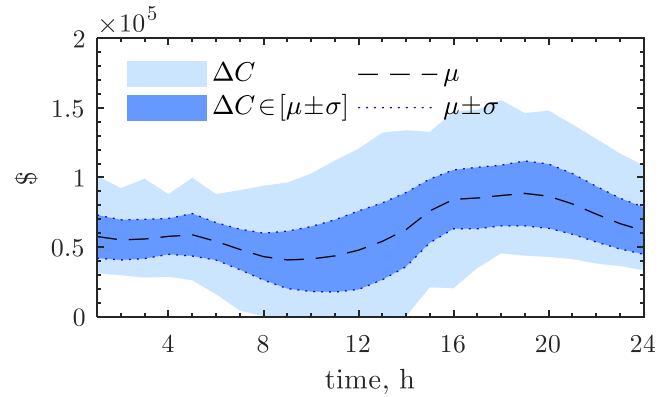
# Results

- Modeling reserves only



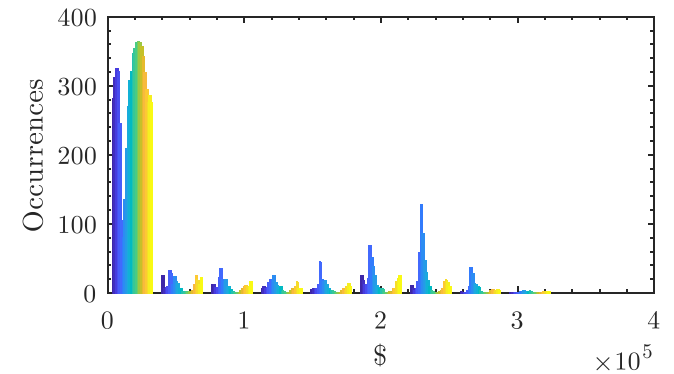
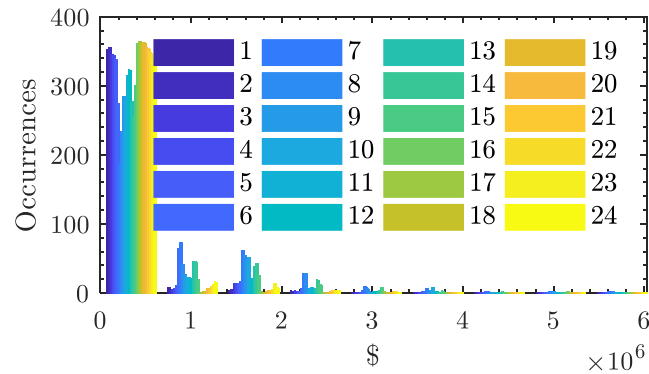
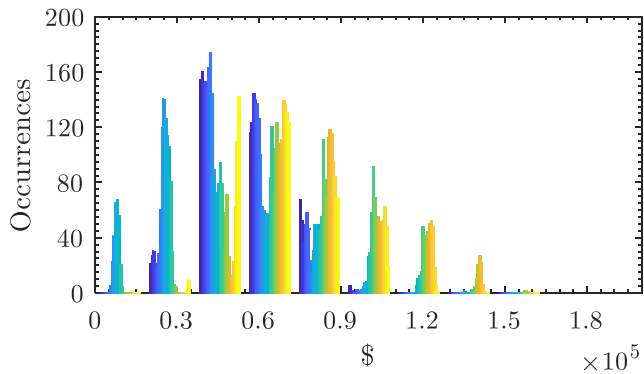
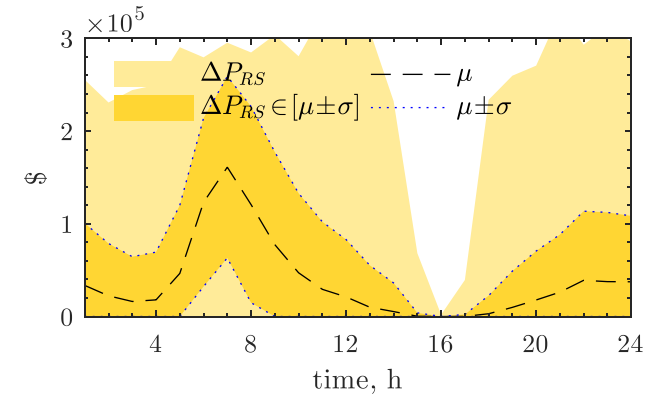
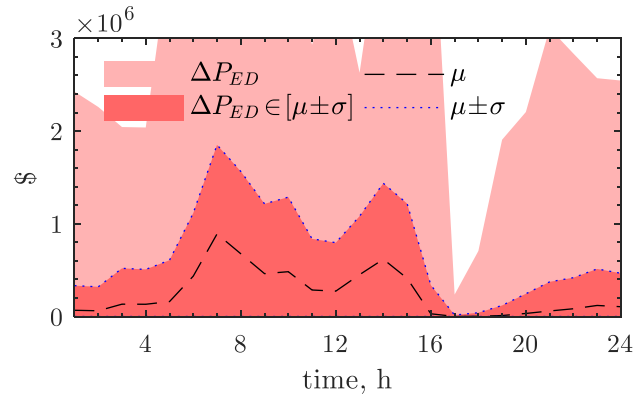
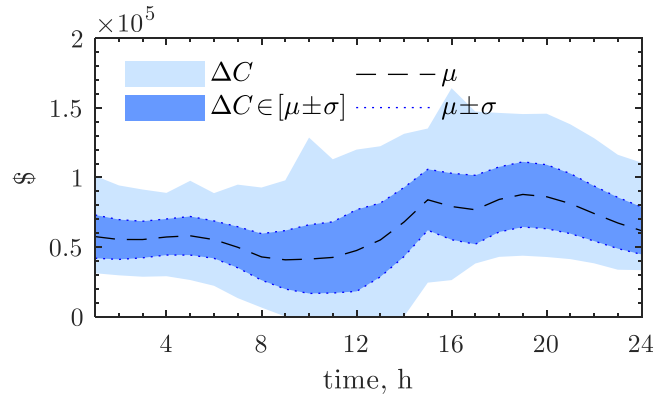
# Results

- Modeling  $P_{\min}$  only

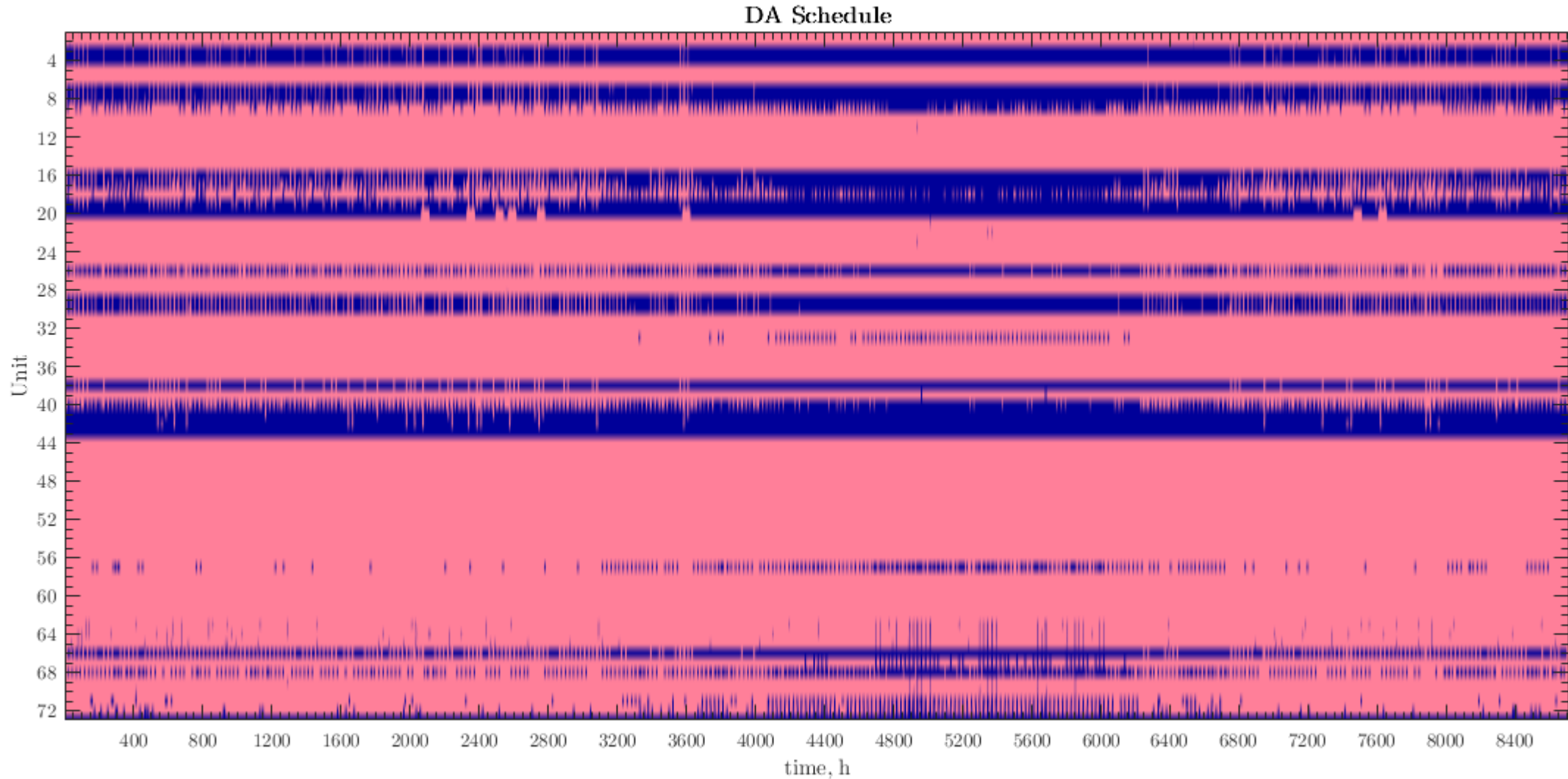


# Results

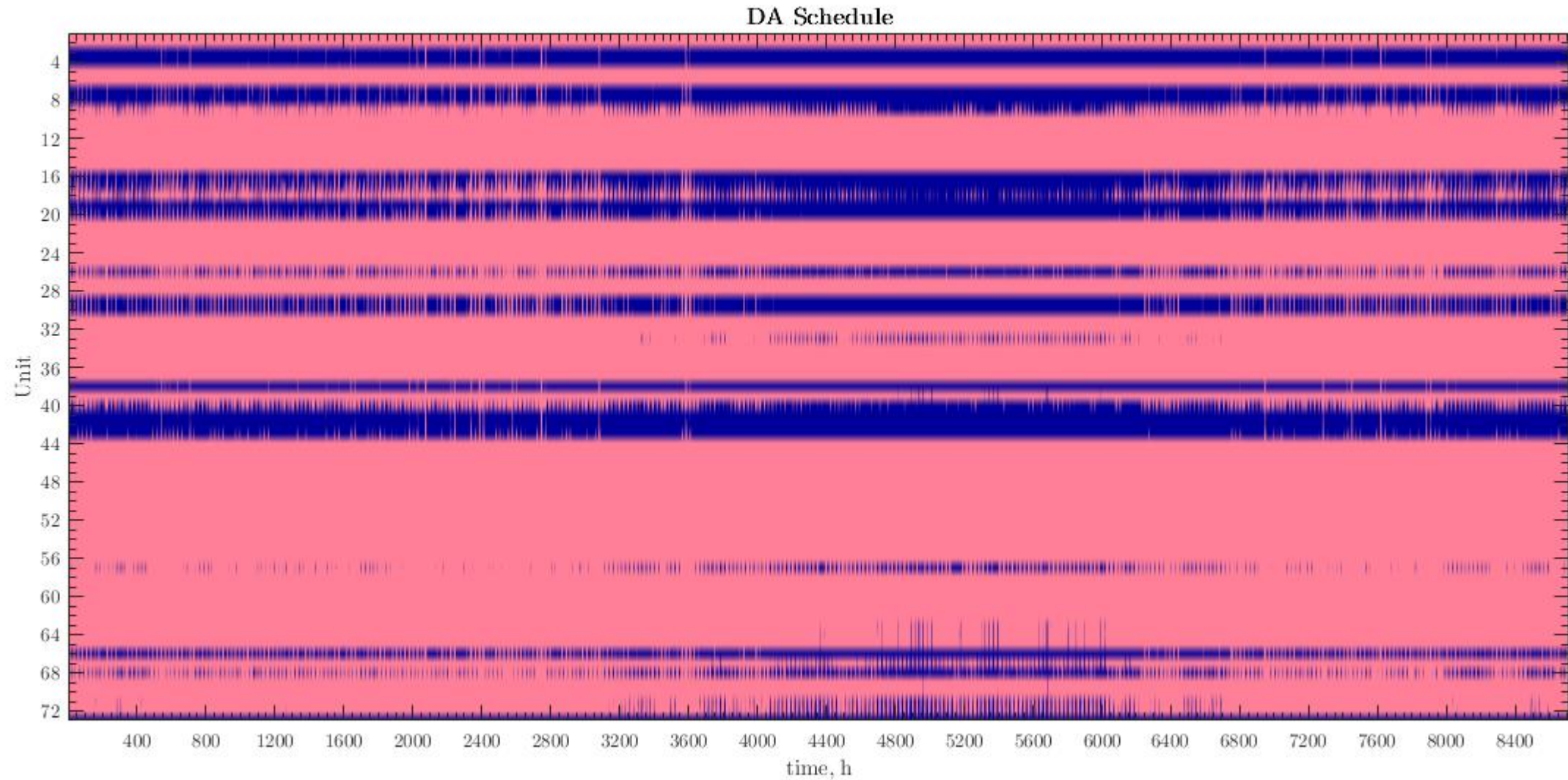
- Modeling Ramps only



# Unit Commitment – min up & down times

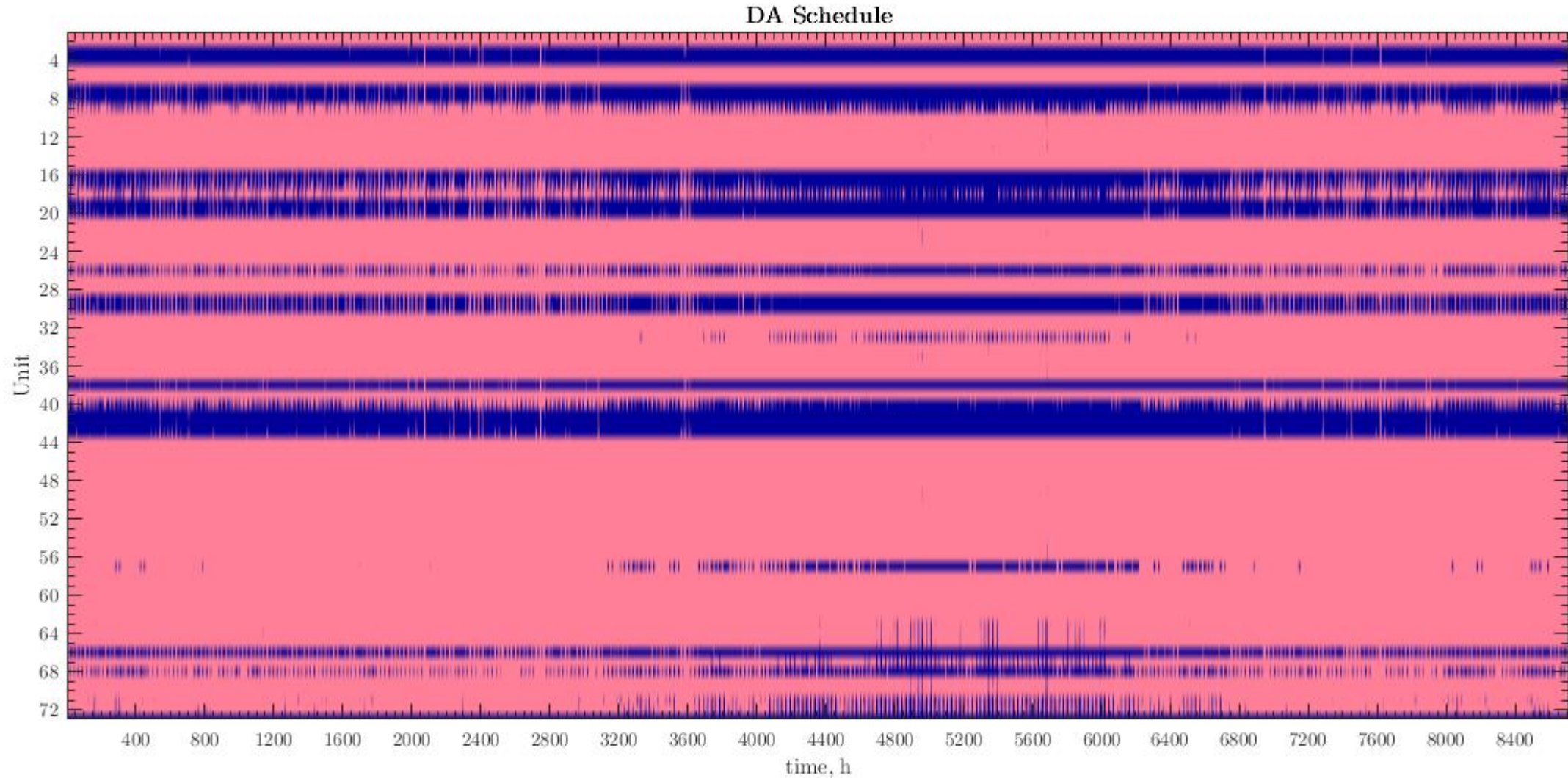


# Unit Commitment – $P_{\min}$ only

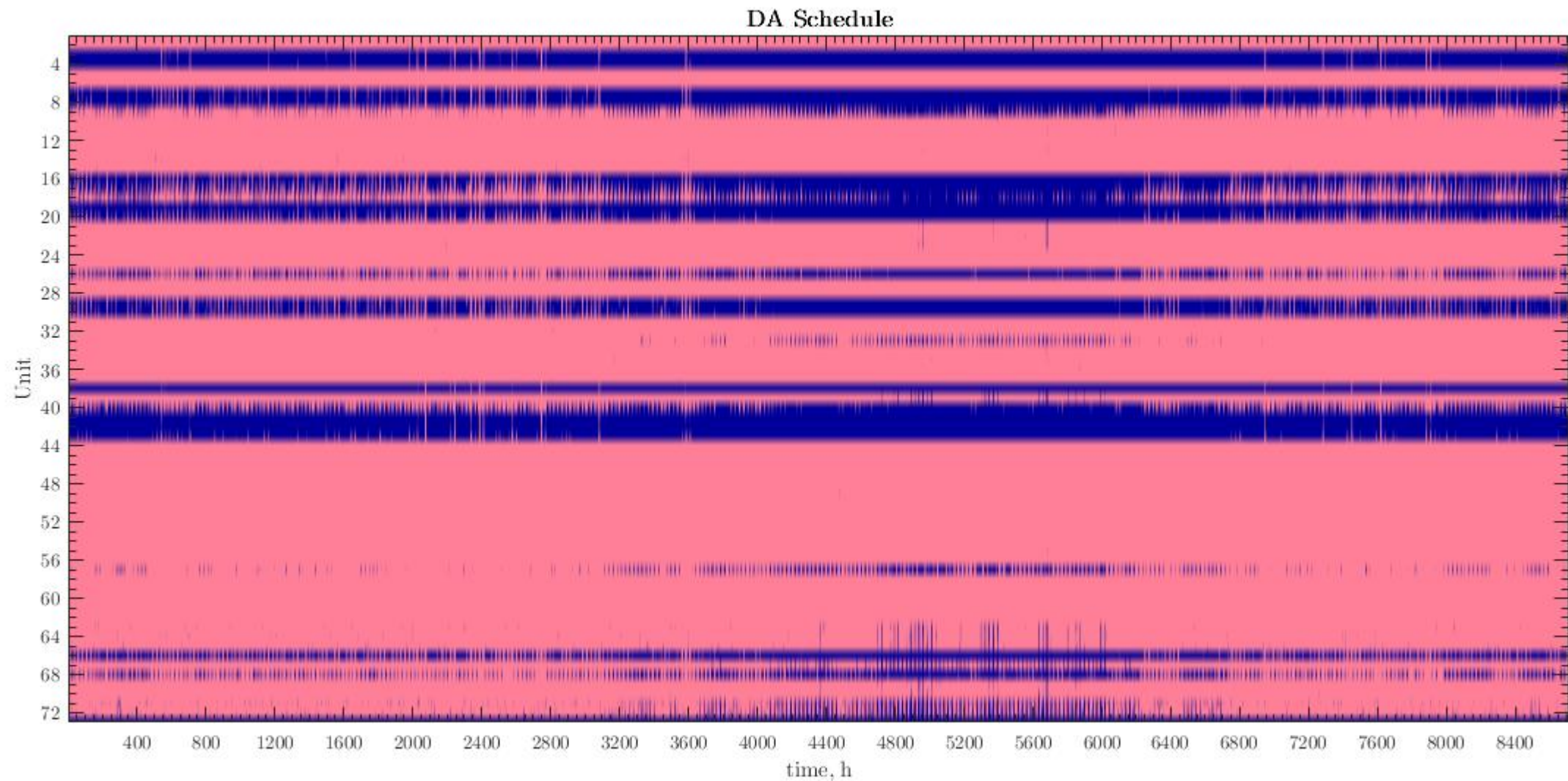




# Unit Commitment – Ramps only

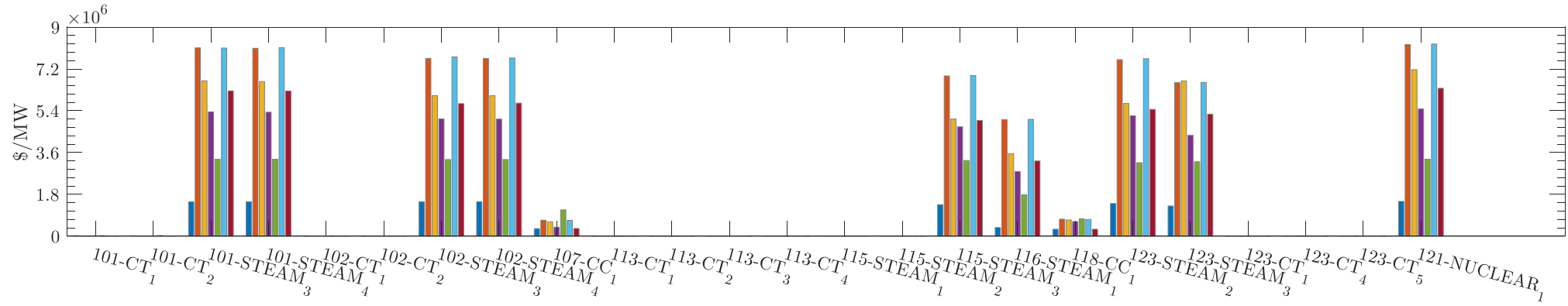


# Unit Commitment – Reserves only

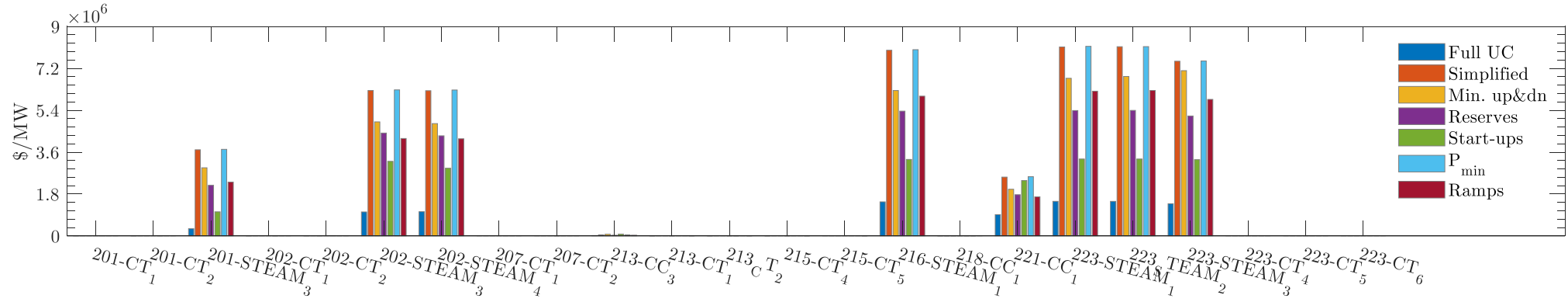


# Units' Revenues

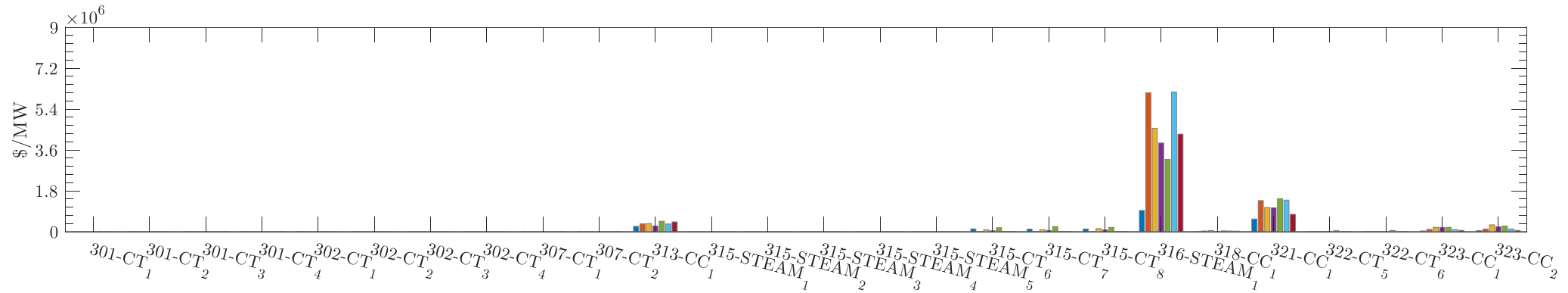
[1:23 73]



[24:46]

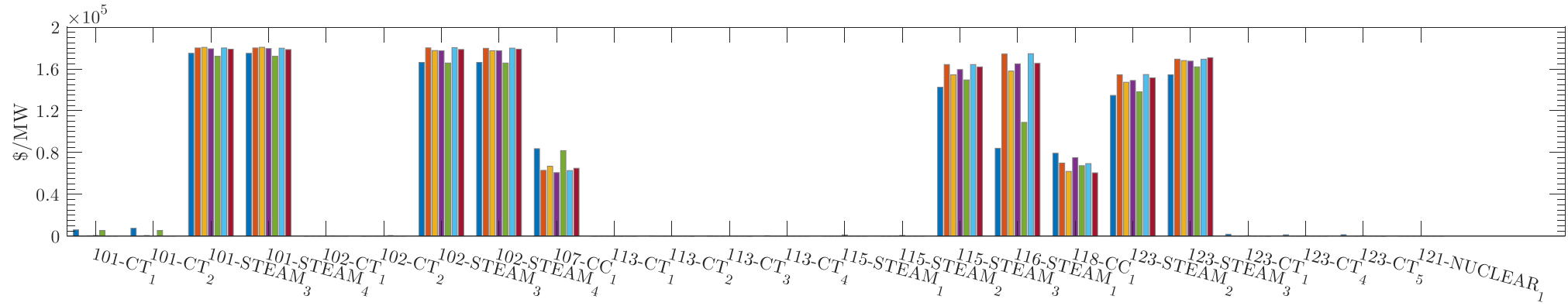


[47:72]

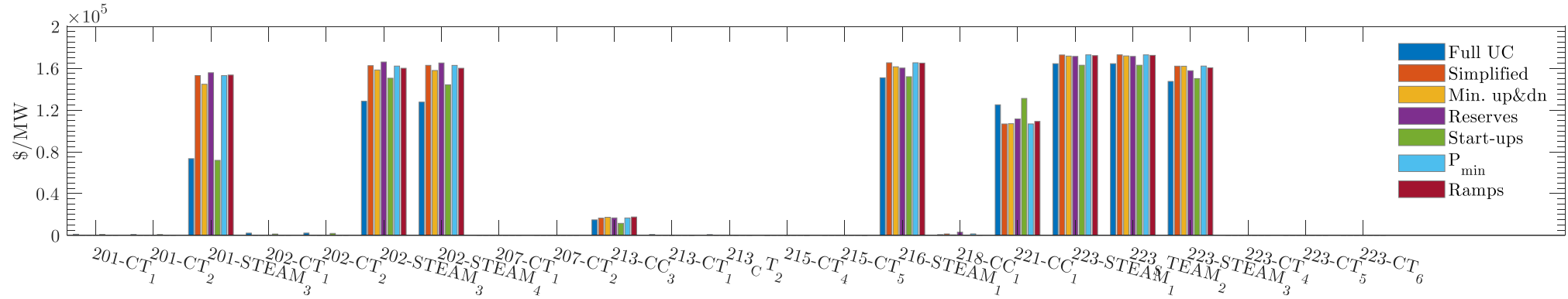


# Units' Costs

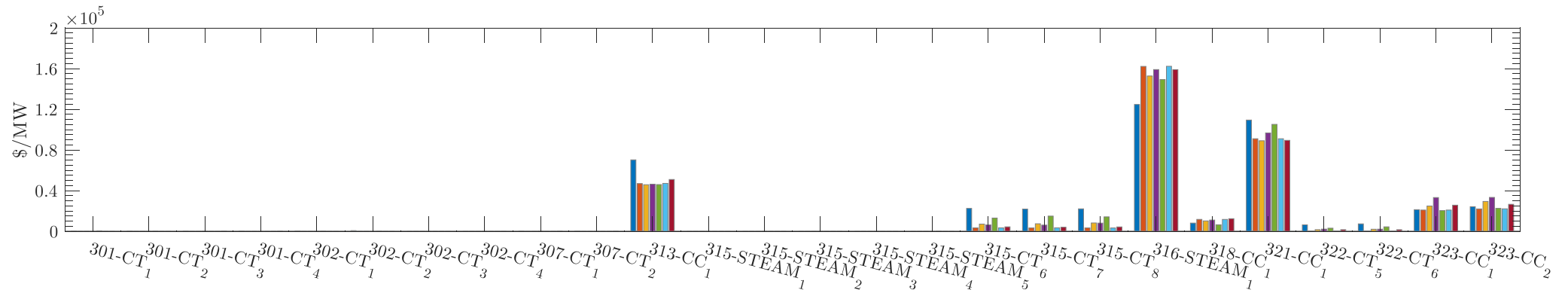
[1:23 73]



[24:46]



[47:72]





# Together...Shaping the Future of Electricity